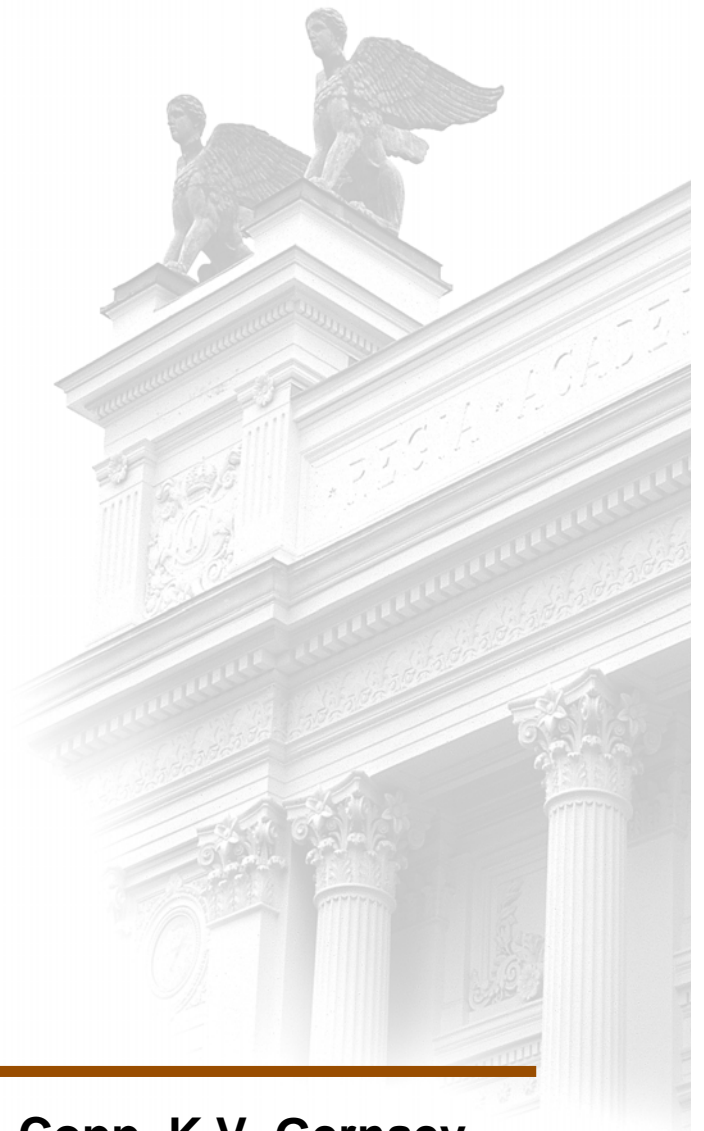


# Benchmark Simulation Model no. 1 (BSM1)



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### **Summary**

The present document presents in details the final state of Benchmark Simulation Model no. 1 (BSM1). The model equations to be implemented for the proposed layout, the procedure to test the implementation and the performance criteria to be used are described, as well as the sensors and control handles. Finally open-loop and closed-loop results obtained with a Matlab-Simulink and a FORTRAN implementations are proposed.

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## 1. Introduction

Wastewater treatment plants (WWTPs) are large non-linear systems subject to large perturbations in influent flow rate and pollutant load, together with uncertainties concerning the composition of the incoming wastewater. Nevertheless these plants have to be operated continuously, meeting stricter and stricter regulations.

Many control strategies have been proposed in the literature but their evaluation and comparison, either practical or based on simulation is difficult. This is due to a number of reasons, including: (1) the variability of the influent; (2) the complexity of the biological and biochemical phenomena; (3) the large range of time constants (varying from a few minutes to several days); (4) the lack of standard evaluation criteria (among other things, due to region specific effluent requirements and cost levels).

It is difficult to judge the particular influence of the applied control strategy on reported plant performance increase, as the reference situation is often not properly characterized. Due to the complexity of the systems it takes much effort to develop alternative controller approaches, and as a consequence of that a fair comparison between different control strategies is only made seldomly. And even if this is done, it remains difficult to conclude to what extent the proposed solution is process or location specific.

To enhance the acceptance of innovating control strategies the performance evaluation should be based on a rigorous methodology including a simulation model, plant layout, controllers, performance criteria and test procedures.

From 1998 to 2004 the development of benchmark tools for simulation-based evaluation of control strategies for activated sludge plants has been undertaken in Europe by Working Groups of COST Action 682 and 624 (Alex *et al.*, 1999). This development work is now continued under the umbrella of the IWA Task Group on Benchmarking of Control Strategies for WWTPs.

The benchmark is a simulation environment defining a plant layout, a simulation model, influent loads, test procedures and evaluation criteria. For each of these items, compromises were pursued to combine plainness with realism and accepted standards. Once the user has validated the simulation code, any control strategy can be applied and the performance can be evaluated according to a defined set of criteria.

The benchmark is not linked to a particular simulation platform: direct coding (C/C++, Fortran) as well as commercial WWTP simulation software packages can be used. For this reason the full set of equations and all the parameter values are available on this website. Tips for implementation of the Benchmark Simulation Model no. 1 (BSM1) on various simulation software platforms are also available in a manual.

The first layout (BSM1) is relatively simple. The benchmark plant is composed of a five-compartment activated sludge reactor consisting of two anoxic tanks followed by three aerobic tanks. The plant thus combines nitrification with predenitrification in a configuration that is commonly used for achieving biological nitrogen removal in full-scale plants. The activated sludge reactor is followed by a secondary settler. A basic control strategy is proposed to test the benchmark: its aim is to control the dissolved oxygen level in the final

compartment of the reactor by manipulation of the oxygen transfer coefficient and to control the nitrate level in the last anoxic tank by manipulation of the internal recycle flow rate.

The purpose of the present document is to describe in details the BSM1 benchmark, as depicted in Figure 1. Further information to facilitate the implementation on various platforms can be found in Copp (2002). However some slight changes have been made since then and a careful reading of the present document is required.

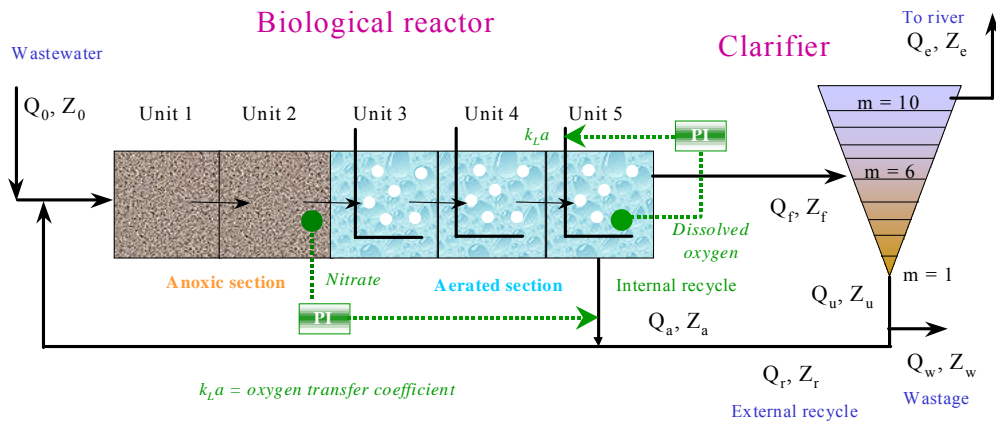


Figure 1: General overview of the BSM1 plant

## 2. Simulation model

### 2.1. General characteristics

The plant is designed for an average influent dry-weather flow rate of  $18,446 \text{ m}^3 \cdot \text{d}^{-1}$  and an average biodegradable COD in the influent of  $300 \text{ g} \cdot \text{m}^{-3}$ . Its hydraulic retention time (based on average dry weather flow rate and total tank volume – i.e. biological reactor + settler – of  $12,000 \text{ m}^3$ ) is 14.4 hours. The biological reactor volume and the settler volume are both equal to  $6,000 \text{ m}^3$ . The wastage flow rate equals  $385 \text{ m}^3 \cdot \text{d}^{-1}$ . This corresponds to a biomass sludge age of about 9 days (based on the total amount of biomass present in the system).

The influent dynamics are defined by means of three files: dry weather, rain weather (a combination of dry weather and a long rain period) and storm weather (a combination of dry weather with two storm events).

### 2.2. Bioprocess model

The Activated Sludge Model no. 1 (ASM1; Henze *et al.*, 1987) has been selected to describe the biological phenomena taking place in the biological reactor (Figure 2).

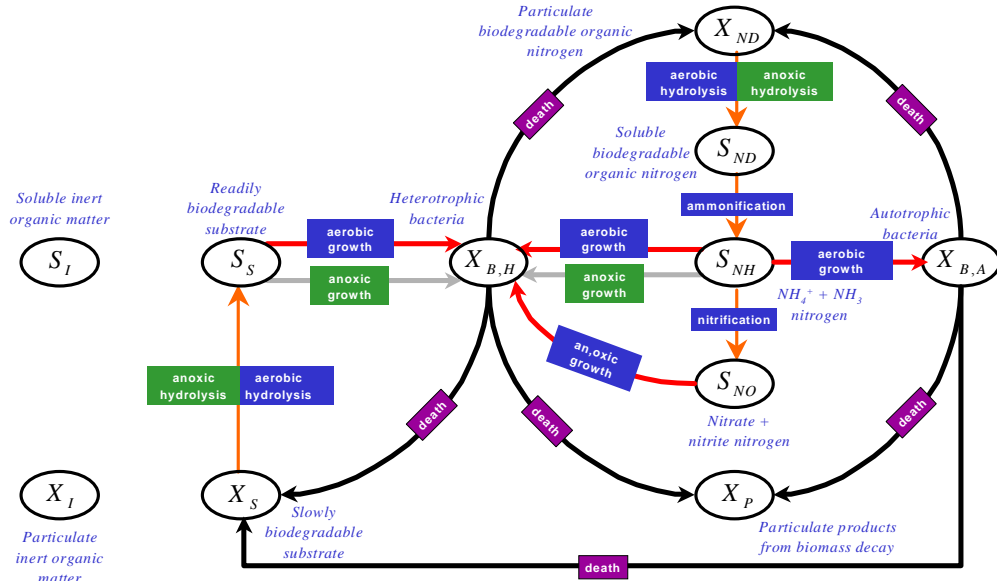


Figure 2: General overview of ASM1

### 2.2.1. List of variables

The list of state variables, with their definition and appropriate notation, is given in Table 1.

Definition	Notation
Soluble inert organic matter	$S_I$
Readily biodegradable substrate	$S_S$
Particulate inert organic matter	$X_I$
Slowly biodegradable substrate	$X_S$
Active heterotrophic biomass	$X_{B,H}$
Active autotrophic biomass	$X_{B,A}$
Particulate products arising from biomass decay	$X_P$
Oxygen	$S_O$
Nitrate and nitrite nitrogen	$S_{NO}$
$\text{NH}_4^+ + \text{NH}_3$ nitrogen	$S_{NH}$
Soluble biodegradable organic nitrogen	$S_{ND}$
Particulate biodegradable organic nitrogen	$X_{ND}$
Alkalinity	$S_{ALK}$

Table 1: List of ASM1 variables

### 2.2.2. List of processes

Eight basic processes are used to describe the biological behavior of the system.

- $j = 1$ : Aerobic growth of heterotrophs

$$\rho_1 = \mu_H \left( \frac{S_S}{K_S + S_S} \right) \left( \frac{S_O}{K_{O,H} + S_O} \right) X_{B,H}$$

- $j = 2$ : Anoxic growth of heterotrophs

$$\rho_2 = \mu_H \left( \frac{S_S}{K_S + S_S} \right) \left( \frac{K_{O,H}}{K_{O,H} + S_O} \right) \left( \frac{S_{NO}}{K_{NO} + S_{NO}} \right) \eta_g X_{B,H}$$

- $j = 3$ : Aerobic growth of autotrophs
 
$$\rho_3 = \mu_A \left( \frac{S_{NH}}{K_{NH} + S_{NH}} \right) \left( \frac{S_O}{K_{O,A} + S_O} \right) X_{B,A}$$
- $j = 4$ : Decay of heterotrophs
 
$$\rho_4 = b_H X_{B,H}$$
- $j = 5$ : Decay of autotrophs
 
$$\rho_5 = b_A X_{B,A}$$
- $j = 6$ : Ammonification of soluble organic nitrogen
 
$$\rho_6 = k_d S_{ND} X_{B,H}$$
- $j = 7$ : Hydrolysis of entrapped organics
 
$$\rho_7 = k_h \frac{X_S / X_{B,H}}{K_X + (X_S / X_{B,H})} \left[ \left( \frac{S_O}{K_{O,H} + S_O} \right) + \eta_h \left( \frac{K_{O,H}}{K_{O,H} + S_O} \right) \left( \frac{S_{NO}}{K_{NO} + S_{NO}} \right) \right] X_{B,H}$$
- $j = 8$ : Hydrolysis of entrapped organic nitrogen
 
$$\rho_8 = k_h \frac{X_S / X_{B,H}}{K_X + (X_S / X_{B,H})} \left[ \left( \frac{S_O}{K_{O,H} + S_O} \right) + \eta_h \left( \frac{K_{O,H}}{K_{O,H} + S_O} \right) \left( \frac{S_{NO}}{K_{NO} + S_{NO}} \right) \right] X_{B,H} (X_{ND} / X_S)$$

### 2.2.3. Observed conversion rates

The observed conversion rates ( $r_i$ ) result from combinations of the basic processes:

$$r_i = \sum_j v_{ij} \rho_j$$

- $S_I (i = 1)$

$$r_1 = 0$$

- $S_S (i = 2)$

$$r_2 = -\frac{1}{Y_H} \rho_1 - \frac{1}{Y_H} \rho_2 + \rho_7$$

- $X_I (i = 3)$

$$r_3 = 0$$

- $X_S (i = 4)$

$$r_4 = (1 - f_P) \rho_4 + (1 - f_P) \rho_5 - \rho_7$$

- $X_{B,H} (i = 5)$

$$r_5 = \rho_1 + \rho_2 - \rho_4$$

- $X_{B,A} (i = 6)$

$$r_6 = \rho_3 - \rho_5$$

- $X_P (i = 7)$

$$r_7 = f_P \rho_4 + f_P \rho_5$$

- $S_O (i = 8)$

$$r_8 = -\frac{1 - Y_H}{Y_H} \rho_1 - \frac{4.57 - Y_A}{Y_A} \rho_3$$

- $S_{NO} (i = 9)$

$$r_9 = -\frac{1 - Y_H}{2.86 Y_H} \rho_2 + \frac{1}{Y_A} \rho_3$$

- $S_{NH}$  ( $i = 10$ )

$$r_{10} = -i_{XB}\rho_1 - i_{XB}\rho_2 - \left(i_{XB} + \frac{1}{Y_A}\right)\rho_3 + \rho_6$$

- $S_{ND}$  ( $i = 11$ )

$$r_{11} = -\rho_6 + \rho_8$$

- $X_{ND}$  ( $i = 12$ )

$$r_{12} = (i_{XB} - f_P i_{XP})\rho_4 + (i_{XB} - f_P i_{XP})\rho_5 - \rho_8$$

- $S_{ALK}$  ( $i = 13$ )

$$r_{13} = -\frac{i_{XB}}{14}\rho_1 + \left(\frac{1 - Y_H}{14 \cdot 2.86 Y_H} - \frac{i_{XB}}{14}\right)\rho_2 - \left(\frac{i_{XB}}{14} + \frac{1}{7Y_A}\right)\rho_3 + \frac{1}{14}\rho_6$$

#### 2.2.4. Biological parameter values

The biological parameter values used in the BSM1 correspond approximately to a temperature of 15°C. The stoichiometric parameters are listed in Table 2 and the kinetic parameters in Table 3.

Parameter	Unit	Value
$Y_A$	g cell COD formed.(g N oxidized) <sup>-1</sup>	0.24
$Y_H$	g cell COD formed.(g COD oxidized) <sup>-1</sup>	0.67
$f_P$	dimensionless	0.08
$i_{XB}$	g N.(g COD) <sup>-1</sup> in biomass	0.08
$i_{XP}$	g N.(g COD) <sup>-1</sup> in particulate products	0.06

Table 2: Stoichiometric parameters

Parameter	Unit	Value
$\mu_H$	d <sup>-1</sup>	4.0
$K_S$	g COD.m <sup>-3</sup>	10.0
$K_{O,H}$	g (-COD).m <sup>-3</sup>	0.2
$K_{NO}$	g NO <sub>3</sub> -N.m <sup>-3</sup>	0.5
$b_H$	d <sup>-1</sup>	0.3
$\eta_g$	dimensionless	0.8
$\eta_h$	dimensionless	0.8
$k_h$	g slowly biodegradable COD.(g cell COD . d) <sup>-1</sup>	3.0
$K_X$	g slowly biodegradable COD.(g cell COD) <sup>-1</sup>	0.1
$\mu_A$	d <sup>-1</sup>	0.5
$K_{NH}$	g NH <sub>3</sub> -N.m <sup>-3</sup>	1.0
$b_A$	d <sup>-1</sup>	0.05
$K_{O,A}$	g (-COD).m <sup>-3</sup>	0.4
$k_a$	m <sup>3</sup> .(g COD . d) <sup>-1</sup>	0.05

Table 3: Kinetic parameters

### 2.3. Detailed plant layout

#### 2.3.1. Bioreactor (General characteristics)

According to Figure 1, the general characteristics of the bioreactor for the default case are:



Number of compartments: 5

Non-aerated compartments: compartments 1-2

Aerated compartments:

- compartments 3-4, with a fixed oxygen transfer coefficient ( $K_{La} = 10 \text{ h}^{-1} = 240 \text{ d}^{-1}$ )
- compartment 5: the dissolved oxygen concentration (DO) is controlled at a level of  $2 \text{ g (-COD).m}^{-3}$  by manipulation of the  $K_{La}$

For each compartment:

- Flow rate:  $Q_k$
- Concentration:  $Z_k$
- Volume:
  - Non-aerated compartments:  $V_1 = V_2 = 1,000 \text{ m}^3$
  - Aerated compartments:  $V_3 = V_4 = V_5 = 1,333 \text{ m}^3$
- Reaction rate:  $r_k$

### 2.3.2. Reactor mass balances (general formula)

The general equations for mass balancing are as follows:

- For  $k = 1$  (unit 1)

$$\frac{dZ_1}{dt} = \frac{1}{V_1} (Q_a Z_a + Q_r Z_r + Q_0 Z_0 + r_1 V_1 - Q_1 Z_1)$$

$$Q_1 = Q_a + Q_r + Q_0$$

- For  $k = 2$  to 5

$$\frac{dZ_k}{dt} = \frac{1}{V_k} (Q_{k-1} Z_{k-1} + r_k V_k - Q_k Z_k)$$

$$Q_k = Q_{k-1}$$

- Special case for oxygen ( $S_{O,k}$ )

$$\frac{dS_{O,k}}{dt} = \frac{1}{V_k} (Q_{k-1} S_{O,k-1} + r_k V_k + (K_{La})_k V_k (S_o^* - S_{O,k}) - Q_k S_{O,k})$$

where the saturation concentration for oxygen is  $S_o^* = 8 \text{ g.m}^{-3}$ .

- Miscellaneous

$$Z_a = Z_5$$

$$Z_f = Z_5$$

$$Z_w = Z_r$$

$$Q_f = Q_5 - Q_a = Q_e + Q_r + Q_w = Q_e + Q_u$$

### 2.3.3. Secondary settler

The secondary settler is modeled as a 10 layers non-reactive unit (i.e. no biological reaction). The 6<sup>th</sup> layer (counting from bottom to top) is the feed layer. The settler has an area (A) of  $1,500 \text{ m}^2$ . The height of each layer  $m$  ( $z_m$ ) is equal to  $0.4 \text{ m}$ , for a total height of  $4 \text{ m}$ . Therefore the settler volume is equal to  $6,000 \text{ m}^3$ .

The solid flux due to gravity is  $J_s = v_s(X)X$  where  $X$  is the total sludge concentration. A double-exponential settling velocity function (Takács *et al.*, 1991) has been selected:

$$v_s(X) = \max\left[0, \min\left\{v'_0, v_0\left(e^{-r_h(X-X_{\min})} - e^{-r_p(X-X_{\min})}\right)\right\}\right]$$

with  $X_{\min} = f_{ns} X_f$ . The parameter values for the settling velocity function are given in Table 4.

	Parameter	Units	Value
Maximum settling velocity	$v'_0$	m.d <sup>-1</sup>	250.0
Maximum Vesilind settling velocity	$v_0$	m.d <sup>-1</sup>	474
Hindered zone settling parameter	$r_h$	m <sup>3</sup> .(g SS) <sup>-1</sup>	0.000576
Flocculant zone settling parameter	$r_p$	m <sup>3</sup> .(g SS) <sup>-1</sup>	0.00286
Non-settleable fraction	$f_{ns}$	dimensionless	0.00228

Table 4: Settling parameters

According to these notations, the mass balances for the sludge are written as:

- For the feed layer ( $m = 6$ )

$$\frac{dX_m}{dt} = \frac{\frac{Q_f X_f}{A} + J_{clar,m+1} - (v_{up} - v_{dn})X_m - \min(J_{s,m}, J_{s,m-1})}{z_m}$$

- For the intermediate layers below the feed layer ( $m = 2$  to  $m = 5$ )

$$\frac{dX_m}{dt} = \frac{v_{dn}(X_{m+1} - X_m) + \min(J_{s,m}, J_{s,m+1}) - \min(J_{s,m}, J_{s,m-1})}{z_m}$$

- For the bottom layer ( $m = 1$ )

$$\frac{dX_1}{dt} = \frac{v_{dn}(X_2 - X_1) + \min(J_{s,2}, J_{s,1})}{z_1}$$

- For the intermediate clarification layers above the feed layer ( $m = 7$  to  $m = 9$ )

$$\frac{dX_m}{dt} = \frac{v_{up}(X_{m-1} - X_m) + J_{clar,m+1} - J_{clar,m}}{z_m}$$

$$J_{clar,j} = \begin{cases} \min(v_{s,j} X_j, v_{s,j-1} X_{j-1}) & \text{if } X_{j-1} > X_t \\ \text{or} \\ v_{s,j} X_j & \text{if } X_{j-1} \leq X_t \end{cases}$$

- For the top layer ( $m = 10$ )

$$\frac{dX_{10}}{dt} = \frac{v_{up}(X_9 - X_{10}) - J_{clar,10}}{z_{10}}$$

$$\text{with } J_{clar,10} = \begin{cases} \min(v_{s,10}X_{10}, v_{s,9}X_9) & \text{if } X_9 > X_t \\ \text{or} \\ v_{s,10}X_{10} & \text{if } X_9 \leq X_t \end{cases}$$

The threshold concentration  $X_t$  is equal to  $3,000 \text{ g.m}^{-3}$

For the soluble components (including dissolved oxygen), each layer represents a completely mixed volume and the concentrations of soluble components are accordingly:

- For the feed layer ( $m = 6$ )

$$\frac{dZ_m}{dt} = \frac{Q_f Z_f - (v_{dn} + v_{up})Z_m}{z_m}$$

- For the layers  $m = 1$  to  $5$

$$\frac{dZ_m}{dt} = \frac{v_{dn}(Z_{m+1} - Z_m)}{z_m}$$

- For the layers  $m = 7$  to  $10$

$$\frac{dZ_m}{dt} = \frac{v_{up}(Z_{m-1} - Z_m)}{z_m}$$

$$v_{dn} = \frac{Q_u}{A} = \frac{Q_r + Q_w}{A}$$

$$v_{up} = \frac{Q_e}{A}$$

The concentrations in the recycle and wastage flow are equal to those of the 1<sup>st</sup> layer (bottom layer):

$$Z_u = Z_1$$

To calculate the sludge concentration from the concentrations in compartment 5 of the activated sludge reactor:

$$X_f = \frac{1}{fr_{COD-SS}} (X_{S,5} + X_{P,5} + X_{I,5} + X_{B,H,5} + X_{B,A,5}) = 0.75(X_{S,5} + X_{P,5} + X_{I,5} + X_{B,H,5} + X_{B,A,5})$$

as  $fr_{COD-SS} = 4/3$ . The same principle is applied for  $X_u$  (in the settler underflow) and  $X_e$  (at the plant exit).

To calculate the distribution of particulate concentrations in the recycle and the wastage flows, their ratios with respect to the total solid concentration are assumed to remain constant across the settler:

$$\frac{X_{S,5}}{X_f} = \frac{X_{S,u}}{X_u}$$

Similar equations hold for  $X_{P,u}$ ,  $X_{I,u}$ ,  $X_{B,H,u}$ ,  $X_{B,A,u}$  and  $X_{ND,u}$ . Note that this assumption means that the dynamics of the fractions of particulate concentrations in the inlet of the settler will be directly propagated to the settler underflow and overflow, without taking into account the normal retention time in the settler.

In the steady-state case the sludge age calculation is based on the total amount of biomass present in the system, i.e. the reactor and the settler:

$$Age = \frac{TX_a + TX_s}{\phi_e + \phi_w}$$

where  $TX_a$  is the total amount of biomass present in the reactor:

$$TX_a = \sum_{i=1}^{i=n} (X_{B,H,i} + X_{B,A,i}) \cdot V_i \text{ with } n = 5$$

$TX_s$  is the total amount of biomass present in the settler:

$$TX_s = \sum_{j=1}^{j=m} (X_{B,H,j} + X_{B,A,j}) \cdot z_j \cdot A \text{ with } m = 10$$

$\phi_e$  is the loss rate of biomass in the effluent:

$$\phi_e = (X_{B,H,m} + X_{B,A,m}) \cdot Q_e$$

with  $m = 10$  and  $\phi_w$  is the loss rate of biomass in the wastage flow

$$\phi_w = (X_{B,H,u} + X_{B,A,u}) \cdot Q_w$$

In an actual plant the sludge age is measured based on the total amount of solids present in the system.

$$Age_{meas} = \frac{TX_{fa} + TX_{fs}}{\phi_{fe} + \phi_{fw}}$$

where  $TX_{fa}$  is the total amount of solids present in the reactor:

$$TX_{fa} = \sum_{i=1}^{i=n} X_{f,i} \cdot V_i$$

with  $n = 5$  and  $X_{f,i} = \frac{1}{fr_{COD-SS}} (X_{S,i} + X_{P,i} + X_{I,i} + X_{B,H,i} + X_{B,A,i})$

$TX_{fs}$  is the total amount of solids present in the settler:

$$TX_{fs} = \sum_{j=1}^{j=m} X_{f,j} \cdot z_j \cdot A$$

with  $m = 10$  and  $X_{f,j} = \frac{1}{fr_{COD-SS}} (X_{S,j} + X_{P,j} + X_{I,j} + X_{B,H,j} + X_{B,A,j})$

$\phi_{fe}$  is the loss rate of solids in the effluent:

$$\phi_{fe} = X_{f,m} \cdot Q_e$$

with  $X_{f,m} = \frac{1}{fr_{COD-SS}} (X_{S,m} + X_{P,m} + X_{I,m} + X_{B,H,m} + X_{B,A,m})$  for  $m = 10$ , and  $\phi_w$  is the loss rate of solids in the wastage flow:

$$\phi_w = X_{f,u} \cdot Q_w$$

with  $X_{f,u} = \frac{1}{fr_{COD-SS}} (X_{S,u} + X_{P,u} + X_{I,u} + X_{B,H,u} + X_{B,A,u})$

## 2.4. Influent data

The influent data were initially proposed by Vanhooren and Nguyen (1996). The time is given in days, the flow rate is given in  $m^3 \cdot d^{-1}$  and the concentrations are given in  $g \cdot m^{-3}$ . The data are given in the following order:

time  $S_I$   $S_S$   $X_I$   $X_S$   $X_{B,H}$   $X_{B,A}$   $X_P$   $S_O$   $S_{NO}$   $S_{NH}$   $S_{ND}$   $X_{ND}$   $S_{ALK}$   $Q_0$

In any influent:  $S_O = 0$  g (-COD).m<sup>-3</sup>;  $X_{B,A} = 0$  g COD.m<sup>-3</sup>;  $S_{NO} = 0$  g N.m<sup>-3</sup>;  $X_P = 0$  g COD.m<sup>-3</sup>;  $S_{ALK} = 7$  mol.m<sup>-3</sup>

#### 2.4.1. Dry weather

The influent file “Inf\_dry\_2006.txt” can be downloaded from the website (<http://www.benchmarkWWTP.org/>). This file contains two weeks of dynamic dry weather influent data (Figure 3).

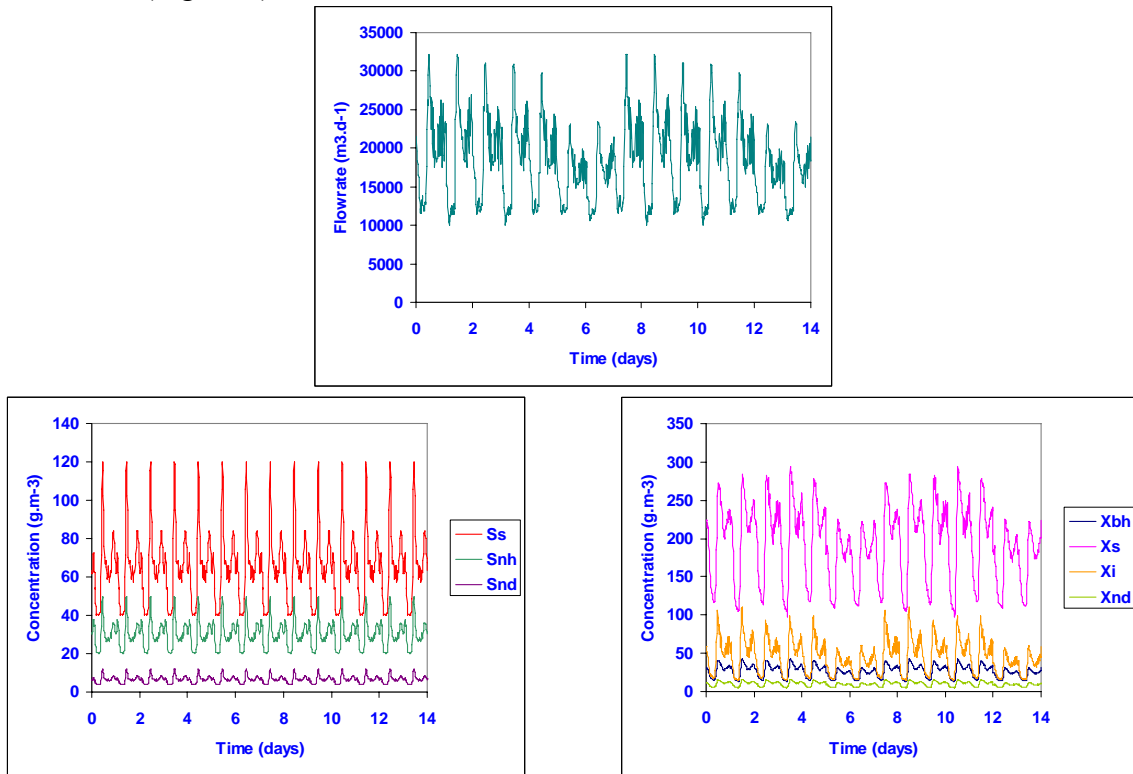


Figure 3: Dry weather influent

#### 2.4.2. Storm weather

The influent file “Inf\_strm\_2006.txt” can be downloaded from the website (<http://www.benchmarkWWTP.org/>). This file contains one week of dynamic dry weather influent data and two storm events superimposed on the dry weather data during the second week (Figure 4).

#### 2.4.3. Rain weather

The influent file “Inf\_rain\_2006.txt” can be downloaded from the website (<http://www.benchmarkWWTP.org/>). This file contains one week of dynamic dry weather data and a long rain event during the second week (Figure 5).

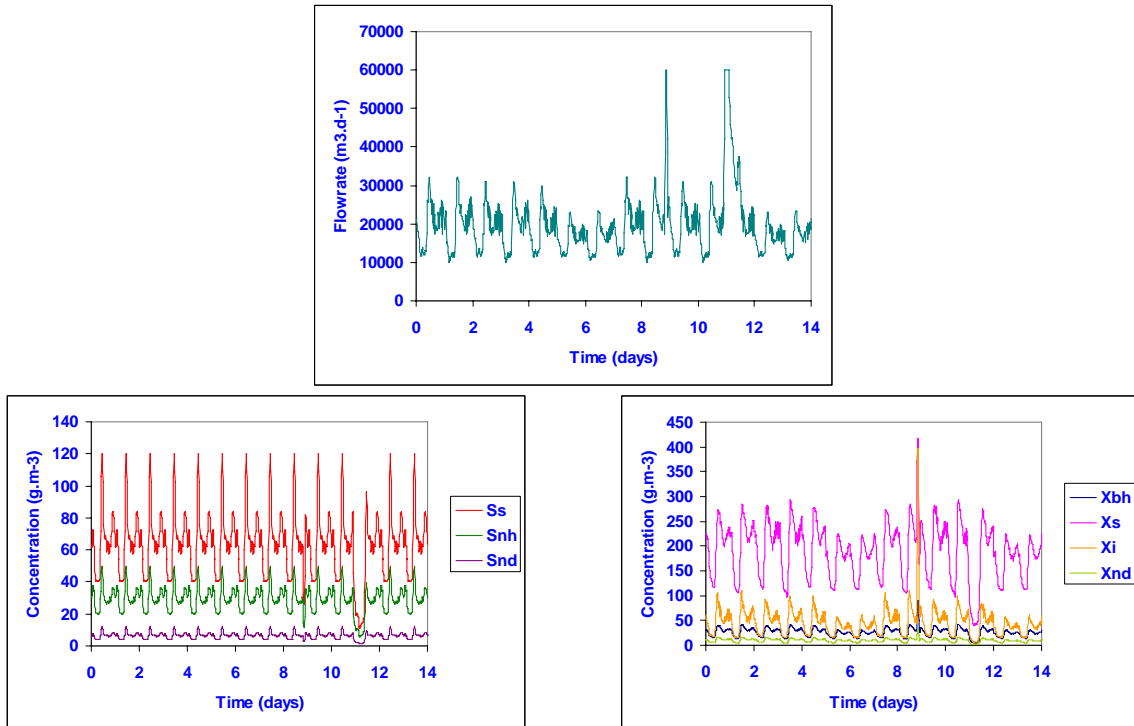


Figure 4: Storm weather influent

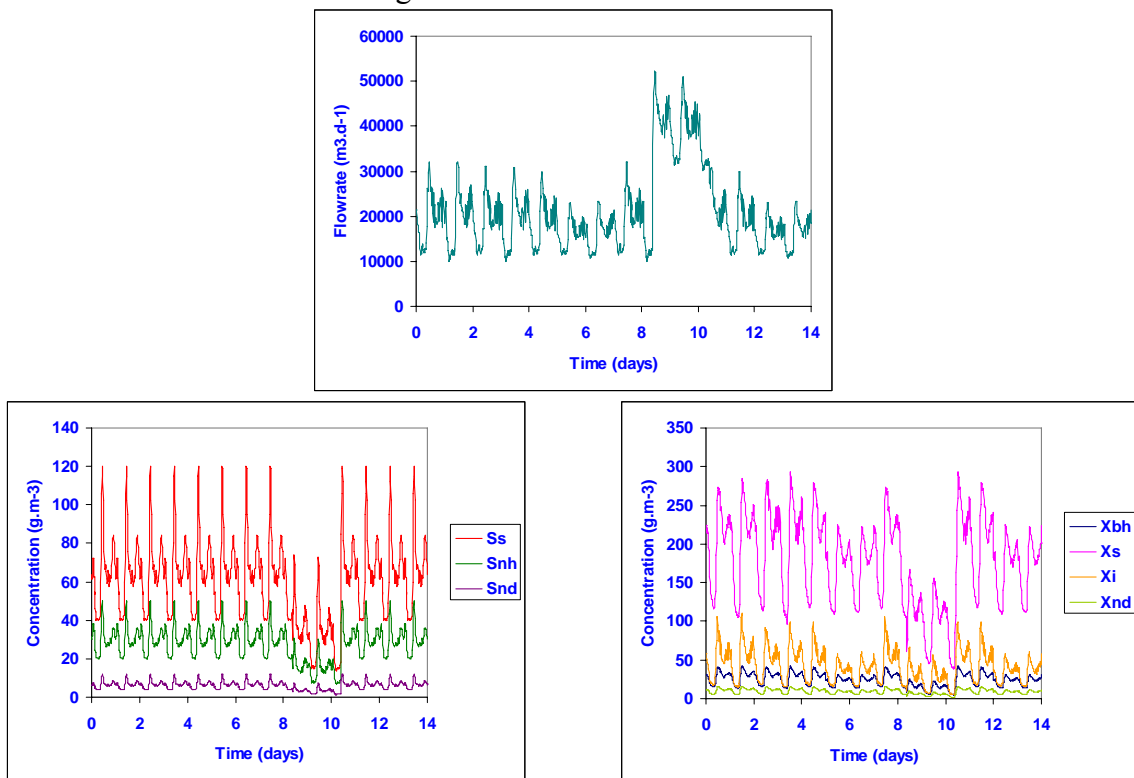


Figure 5: Rain weather influent

### 3. Initialization

Initial values can be selected by the user. A 100-days period of stabilization in closed-loop using constant inputs (average dry weather flow rate, flow-weighted average influent concentrations) with no noise on the measurements has to be completed before using the dry

weather file (14 days) followed by the weather file to be tested. Noise on measurements should be used with the dynamic files. The dynamic load averages to be used as inputs during the stabilization period are given in Table 5 (remaining variables are set to 0).

Variable	Value	Unit
$Q_{0,stab}$	18 446	$\text{m}^3 \cdot \text{d}^{-1}$
$S_{S,stab}$	69.50	$\text{g COD} \cdot \text{m}^{-3}$
$X_{B,H,stab}$	28.17	$\text{g COD} \cdot \text{m}^{-3}$
$X_{S,stab}$	202.32	$\text{g COD} \cdot \text{m}^{-3}$
$X_{I,stab}$	51.20	$\text{g COD} \cdot \text{m}^{-3}$
$S_{NH,stab}$	31.56	$\text{g N} \cdot \text{m}^{-3}$
$S_{I,stab}$	30.00	$\text{g COD} \cdot \text{m}^{-3}$
$S_{ND,stab}$	6.95	$\text{g N} \cdot \text{m}^{-3}$
$X_{ND,stab}$	10.59	$\text{g N} \cdot \text{m}^{-3}$
$S_{ALK}$	7.00	$\text{mol} \cdot \text{m}^{-3}$

Table 5: Load averages for the stabilization period

The system is stabilized if the steady state for these conditions is reached. A simulation period of 10 times the sludge age suffices for that. If for some control strategy the sludge age is influenced, the stabilization period must be adjusted accordingly but in principle the wastage flow rate should not be manipulated for the short-term evaluation of this benchmark.

#### 4. Open-loop assessment

In order for users to verify their implementations, open-loop results for the dry weather situation are available on the website. The procedure to assess the open-loop case is similar to the closed-loop one: simulate the plant for a stabilization period of 100 days before using the dry weather file. For open-loop assessment the default case control variables (see section 5 for full description) have the following constant values:  $Q_a = 55,338 \text{ m}^3 \cdot \text{d}^{-1}$  and  $K_{La}(5) = 3.5 \text{ h}^{-1}$  (or  $84 \text{ d}^{-1}$ ). The steady state values after 100 days (Tables 6 to 8) will be found in the text file “Steady.txt” and the first day of the weather file in the text file “First\_day.txt” (results with 15 minutes sampling interval) on the website (<http://www.benchmarkwwtp.org>). The steady-state and first-day values have been provided by Ulf Jeppsson and were obtained by implementing the benchmark in Matlab/Simulink. A comparison of the steady-state results obtained on three platforms (Matlab/Simulink, GPS-X and FORTRAN code) can be found in Pons *et al.* (1999).

For evaluation of the simulation results over a fixed period of time ( $T = t_f - t_0$ ), average values are to be calculated as follows (The user should be aware that all the integrals for performance assessment are calculated by rectangular integration with a time step of 15 min):

- Flow rate ( $\text{m}^3 \cdot \text{d}^{-1}$ ):  $\bar{Q} = \frac{\int_{t_0}^{t_f} Q(t) \cdot dt}{T}$

- Concentration for compound  $Z_k$  (mass.m<sup>-3</sup>) in flow  $Q$  must be flow proportional:

$$\bar{Z}_k = \frac{\int_{t_0}^{t_f} Q(t) \cdot Z(t)_k \cdot dt}{\int_{t_0}^{t_f} Q(t) \cdot dt}$$

	influent	i	1	2	3	4	5	Unit
$S_{L,stab}$	30	$S_{L,i}$	30	30	30	30	30	g COD.m <sup>-3</sup>
$S_{S,stab}$	69.5	$S_{S,i}$	2.81	1.46	1.15	0.995	0.889	g COD.m <sup>-3</sup>
$X_{L,stab}$	51.2	$X_{L,i}$	1149.	1149.	1149.	1149.	1149.	g COD.m <sup>-3</sup>
$X_{S,stab}$	202.32	$X_{S,i}$	82.1	76.4	64.9	55.7	49.3	g COD.m <sup>-3</sup>
$X_{B,H,stab}$	28.17	$X_{B,H,i}$	2552.	2553.	2557.	2559.	2559.	g COD.m <sup>-3</sup>
$X_{B,A,stab}$	0	$X_{B,A,i}$	148.	148.	149.	150.	150.	g COD.m <sup>-3</sup>
$X_{P,stab}$	0	$X_{P,i}$	449.	450.	450.	451.	452.	g COD.m <sup>-3</sup>
$S_{O,stab}$	0	$S_{O,i}$	0.00430	0.0000631	1.72	2.43	0.491	g (-COD).m <sup>-3</sup>
$S_{NO,stab}$	0	$S_{NO,i}$	5.37	3.66	6.54	9.30	10.4	g N.m <sup>-3</sup>
$S_{NH,stab}$	31.56	$S_{NH,i}$	7.92	8.34	5.55	2.97	1.73	g N.m <sup>-3</sup>
$S_{ND,stab}$	6.95	$S_{ND,i}$	1.22	0.882	0.829	0.767	0.688	g N.m <sup>-3</sup>
$X_{ND,stab}$	10.59	$X_{ND,i}$	5.28	5.03	4.39	3.88	3.53	g N.m <sup>-3</sup>
$S_{ALK,stab}$	7	$S_{ALK,i}$	4.93	5.08	4.67	4.29	4.13	mol.m <sup>-3</sup>
$X_{stab}$		$X_i$	3285	3282	3278	3274	3270	g SS.m <sup>-3</sup>
$Q_{0,stab}$	18446	$Q_i$	92230	92230	92230	92230	92230	m <sup>3</sup> .d <sup>-1</sup>

Table 6: Biological reactor steady-state (open-loop)

	$X$	$S_{L,j}$	$S_{S,j}$	$S_{O,j}$	$S_{NO,j}$	$S_{NH,j}$	$S_{ND,j}$	$S_{ALK,j}$
	g COD.m <sup>-3</sup>	g COD.m <sup>-3</sup>	g COD.m <sup>-3</sup>	g COD.m <sup>-3</sup>	g N.m <sup>-3</sup>	g N.m <sup>-3</sup>	g N.m <sup>-3</sup>	mol.m <sup>-3</sup>
10	12.5	30	0.889	0.491	10.4	1.73	0.688	4.13
9	18.1	30	0.889	0.491	10.4	1.73	0.688	4.13
8	29.5	30	0.889	0.491	10.4	1.73	0.688	4.13
7	69.0	30	0.889	0.491	10.4	1.73	0.688	4.13
6	356.	30	0.889	0.491	10.4	1.73	0.688	4.13
5	356.	30	0.889	0.491	10.4	1.73	0.688	4.13
4	356.	30	0.889	0.491	10.4	1.73	0.688	4.13
3	356.	30	0.889	0.491	10.4	1.73	0.688	4.13
2	356.	30	0.889	0.491	10.4	1.73	0.688	4.13
1	6394.	30	0.889	0.491	10.4	1.73	0.688	4.13

Table 7: Settler steady-state – Concentration of solids and soluble components in the settler layers (open-loop)

## 5. Set-up of default controllers

These default controllers are proposed so the closed-loop simulation and the implementation of the evaluation criteria can be tested before the user implements his/her own control strategy. The primary control objectives for the default strategies are to maintain the NO<sub>3</sub>-N concentration in the 2<sup>nd</sup> compartment at a predetermined set point value (1 g.m<sup>-3</sup>) and the dissolved oxygen concentration in the 5<sup>th</sup> compartment at a predetermined set point value (2 g (-COD).m<sup>-3</sup>). The modeling principles of the sensors are given in Section 7 of this document.



$S_{L,u}$	30	$S_{L,e}$	30	Unit
$S_{S,u}$	0.889	$S_{S,e}$	0.889	g COD.m <sup>-3</sup>
$X_{L,u}$	2247	$X_{L,e}$	4.39	g COD.m <sup>-3</sup>
$X_{S,u}$	96.4	$X_{S,e}$	0.188	g COD.m <sup>-3</sup>
$X_{B,H,u}$	5005	$X_{B,H,e}$	9.78	g COD.m <sup>-3</sup>
$X_{B,A,u}$	293.	$X_{B,A,e}$	0.573	g COD.m <sup>-3</sup>
$X_{P,u}$	884.	$X_{P,e}$	1.73	g COD.m <sup>-3</sup>
$S_{O,u}$	0.491	$S_{O,e}$	0.491	g COD.m <sup>-3</sup>
$S_{NO,u}$	10.4	$S_{NO,u}$	10.4	g N.m <sup>-3</sup>
$S_{NH,u}$	1.73	$S_{NH,e}$	1.73	g N.m <sup>-3</sup>
$S_{ND,u}$	0.688	$S_{ND,e}$	0.688	g N.m <sup>-3</sup>
$X_{ND,u}$	6.90	$X_{ND,e}$	0.0135	g N.m <sup>-3</sup>
$S_{ALK,u}$	4.13	$S_{ALK,e}$	4.13	mol.m <sup>-3</sup>
$X_u$	6394.	$X_e$	12.50	g SS.m <sup>-3</sup>
$Q_r$	18446	$Q_e$	18061	m <sup>3</sup> .d <sup>-1</sup>
$Q_w$	385			m <sup>3</sup> .d <sup>-1</sup>

Table 8: Settler steady-state: State variables at discharge and underflow

### 5.1. Controller variables

The NO<sub>3</sub>-N measurement in compartment 2 is of class B0 with a measurement range of 0 to 20 g N.m<sup>-3</sup>. The minimum value that can be measured by the sensor is 0 g N.m<sup>-3</sup>. The measurement noise is equal to 0.5 g N.m<sup>-3</sup>. The manipulated variable is the internal recycle flow rate from compartment 5 back to compartment 1.

For the DO control in compartment 5, the DO probe is assumed to be of class A with a measurement range of 0 to 10 g (-COD).m<sup>-3</sup> and a measurement noise of 0.25 g (-COD).m<sup>-3</sup>. The manipulated variable is the oxygen transfer coefficient,  $K_{La}(5)$ .

Constraints are applied on recirculation flows. The range for  $Q_a$  is 0 to 5 times  $Q_{0,stab}$ . The external recycle flow rate  $Q_r$  is maintained constant and is set to  $Q_r = Q_{0,stab}$ . There are also constraints on oxygen transfer in compartment 5:  $K_{La} = 0$  to 10 h<sup>-1</sup>.

### 5.2. Controller types

Both suggested controllers are of the PI type. Their performance is assessed by ( $i = 1$  for nitrate-PID and  $i = 2$  for oxygen-PID):

- o IAE (Integral of Absolute Error)

$$IAE_i = \int_{t_0}^{t_f} |e_i| \cdot dt$$

where  $e_i$  is the error:

$$e_i = Z_i^{setpoint} - Z_i^{meas}$$

- o ISE (Integral of Squared Error)

$$ISE_i = \int_{t_0}^{t_f} e_i^2 \cdot dt$$

- o Maximal deviation from set point:

$$Dev_i^{max} = \max\{|e_i|\}$$

- o Variance of error:

$$\text{Var}(e_i) = \overline{e_i^2} - (\overline{e_i})^2$$

with

$$\overline{e_i} = \frac{\int_{t_0}^{t_f} e_i \cdot dt}{T}$$

$$\overline{e_i^2} = \frac{\int_{t_0}^{t_f} e_i^2 \cdot dt}{T}$$

- Variance of manipulated variable ( $u_i$ ) variations:

$$\text{Var}(\Delta u_i) = \overline{\Delta u_i^2} - (\overline{\Delta u_i})^2$$

with

$$\Delta u_i = |u_i(t + dt) - u_i(t)|$$

$$\overline{\Delta u_i} = \frac{\int_{t_0}^{t_f} \Delta u_i \cdot dt}{T}$$

$$\overline{\Delta u_i^2} = \frac{\int_{t_0}^{t_f} \Delta u_i^2 \cdot dt}{T}$$

## 6. Performance assessment

The flow-weighted average values of the effluent concentrations over the three evaluation periods (dry, rain and storm weather: 7 days for each) should obey the limits given in Table 9. Total nitrogen ( $N_{tot}$ ) is calculated as the sum of  $S_{NO,e}$  and  $S_{NKj,e}$ , where  $S_{NKj}$  is the Kjeldahl nitrogen concentration.

Variable	Value
$N_{tot}$	<18 g N.m <sup>-3</sup>
COD <sub>t</sub>	<100 g COD.m <sup>-3</sup>
$S_{NH}$	<4 g N.m <sup>-3</sup>
TSS	<30 g SS.m <sup>-3</sup>
BOD <sub>5</sub>	<10 g BOD.m <sup>-3</sup>

Table 9: Effluent quality limits

The **percentage of time** the effluent limits are not met must be reported, as well as the **number of violations**. The number of violations is defined as the *number of crossings* of the limit (from below to above the limit).

The performance assessment is made at two levels.

- The **first level** concerns the local control loops, assessed by IAE (Integral of the Absolute Error) and ISE (Integral of the Squared Error) criteria, by maximal deviation from set points, and by error variance. Basically, this serves as a proof that the proposed control strategy has been applied properly.

- The **second level** provides measures for the effect of the control strategy as such on plant performance and it can be divided into four sub-levels:

- the **effluent quality**: levies or fines are to be paid due to the discharge of pollution in the receiving water bodies:

The Effluent Quality ( $EQ$ ) (kg pollution unit.d<sup>-1</sup>) is averaged over the period of observation  $T$  (d) (i.e. the second week or 7 last days for each weather file) based on a weighting of the effluent loads of compounds that have a major influence on the quality of the receiving water and that are usually included in regional legislation. It is defined as:

$$EQ = \frac{1}{T \cdot 1000} \int_{t=7 \text{ days}}^{t=14 \text{ days}} \left( B_{SS} \cdot SS_e(t) + B_{COD} \cdot COD_e(t) + B_{NKj} \cdot S_{NKj,e}(t) + B_{NO} \cdot S_{NO,e}(t) + B_{BOD5} \cdot BOD_e(t) \right) Q_e(t) \cdot dt$$

where

$$\begin{aligned} S_{NKj,e} &= S_{NH,e} + S_{ND,e} + X_{ND,e} + i_{XB} (X_{B,H,e} + X_{X,A,e}) + i_{XP} (X_{P,e} + X_{I,e}) \\ SS_e &= 0.75 \cdot (X_{S,e} + X_{I,e} + X_{B,H,e} + X_{B,A,e} + X_{P,e}) \\ BOD_{5,e} &= 0.25 \cdot (S_{S,e} + X_{S,e} + (1 - f_P) \cdot (X_{B,H,e} + X_{B,A,e})) \\ COD_e &= S_{S,e} + S_{I,e} + X_{S,e} + X_{I,e} + X_{B,H,e} + X_{B,A,e} + X_{P,e} \end{aligned}$$

and the  $B_i$  are weighting factors for the different types of pollution to convert them into pollution units (Table 10). The concentrations are to be expressed in g.m<sup>-3</sup>. The values for  $B_i$  have been deduced from Vanrolleghem *et al.* (1996).

Factor	$B_{SS}$	$B_{COD}$	$B_{NKi}$	$B_{NO}$	$B_{BOD5}$
Value (g pollution unit.g <sup>-1</sup> )	2	1	30	10	2

Table 10:  $B_i$  values

The 95% percentiles of the effluent ammonia ( $S_{NH,e95}$ ), effluent total nitrogen ( $N_{tot,e95}$ ) and total suspended solids ( $TSS_{e95}$ ) have to be shown as well. These percentiles represent the  $S_{NH}$ ,  $N_{tot}$  and  $TSS$  effluent concentrations that are exceeded 5% of the time.

- the **cost factors for operation**

- the **sludge production to be disposed** ( $SP$ ) (kg.d<sup>-1</sup>)

The sludge production,  $SP$ , is calculated from the total solid flow from wastage and the solids accumulated in the system over the period of time considered (7 days for each weather file):

Amount of solids in the system at time  $t$ :  $TSS(t)$

$$TSS(t) = TSS_a(t) + TSS_s(t)$$

where  $TSS_a(t)$  is the amount of solids in the reactors:

$$TSS_a(t) = 0.75 \cdot \sum_{i=1}^{i=n} (X_{S,i} + X_{I,i} + X_{B,H,i} + X_{B,A,i} + X_{P,i}) \cdot V_i \text{ with } n = 5$$

$TSS_s(t)$  is the amount of solids in the settler:

$$TSS_s(t) = 0.75 \cdot \sum_{j=1}^{j=m} (X_{S,j} + X_{I,j} + X_{B,H,j} + X_{B,A,j} + X_{P,j}) \cdot z_j \cdot A \text{ with } m = 10$$

$$SP = \frac{1}{T} \left( TSS(14 \text{ days}) - TSS(7 \text{ days}) + 0.75 \cdot \int_{t=7 \text{ days}}^{t=14 \text{ days}} (X_{S,w} + X_{I,u} + X_{B,H,w} + X_{B,A,w}) \cdot Q_w(t) \cdot dt \right)$$

- the **total sludge production** ( $SP_{total}$ ) ( $\text{kg}\cdot\text{d}^{-1}$ ) takes into account the sludge to be disposed and the sludge lost at the weir:

$$SP_{total} = SP + \frac{0.75}{T} \int_{t=7 \text{ days}}^{t=14 \text{ days}} (X_{S,e} + X_{I,e} + X_{B,H,e} + X_{B,A,e} + X_{P,e}) \cdot Q_e(t) dt$$

- the **aeration energy** ( $AE$ ) ( $\text{kWh}\cdot\text{d}^{-1}$ ) and the **pumping energy** ( $PE$ ) ( $\text{kWh}\cdot\text{d}^{-1}$ ) (internal and external flow recycle pumps).

The pumping energy depends on how the various tanks can be arranged on the available space. Considering the state-of-the-art design rules an arrangement with two parallel lines, similar to the one shown in Appendix 1, can be proposed. In BSM1 the pumping energy is calculated as:

$$PE = \frac{1}{T} \int_{t=7 \text{ days}}^{t=14 \text{ days}} (0.004 \cdot Q_a(t) + 0.008 \cdot Q_r(t) + 0.05 \cdot Q_w(t)) \cdot dt \text{ with the flow rates expressed in } \text{m}^3 \cdot \text{d}^{-1}.$$

The aeration energy  $AE$  should take into account the plant peculiarities (type of diffuser, bubble size, depth of submersion, etc ...) and is calculated from the  $k_L a$  according to the following relation, valid for Degrémont DP230 porous disks at an immersion depth of 4 m:

$$AE = \frac{S_O^{sat}}{T \cdot 1.8 \cdot 1000} \int_{7 \text{ days}}^{14 \text{ days}} \sum_{i=1}^5 V_i \cdot K_L a_i(t) dt$$

with  $K_L a$  given in  $\text{d}^{-1}$  and  $i$  referring to the compartment number.

- the **consumption of external carbon source** ( $EC$ ) ( $\text{kg COD}\cdot\text{d}^{-1}$ ) that could be added to improve denitrification (see Section 7 on control and handles)

$$EC = \frac{COD_{EC}}{T \cdot 1000} \int_{t=7 \text{ days}}^{t=14 \text{ days}} \left( \sum_{i=1}^{i=n} q_{EC,i} \right) \cdot dt$$

where  $q_{EC,i}$  is the flow rate of external carbon added to compartment  $i$ ,  $COD_{EC} = 400,000 \text{ g COD}\cdot\text{m}^{-3}$  is the concentration of readily biodegradable substrate in the external carbon source.

- the **mixing energy** ( $ME$ ) ( $\text{kWh}\cdot\text{d}^{-1}$ )

The compartments in anoxic state should be mixed to avoid settling. Mixing energy is a function of the compartment volume.

$$ME = \frac{24}{T} \int_{t=7 \text{ days}}^{t=14 \text{ days}} \sum_{i=1}^{i=5} \left[ \begin{array}{l} 0.005 \cdot V_i \text{ if } K_L a_i(t) < 20 \text{ d}^{-1} \\ 0 \text{ otherwise} \end{array} \right] \cdot dt$$

- controller output variations**

The maximum values and the variance of the manipulated variables variations should be given. This will provide an indication on peak loads and the wear of the pumps and aeration devices.

Furthermore an **Influent Quality** ( $IQ$ ) index can be defined as:

$$IQ = \frac{1}{T \cdot 1000} \int_{t=7 \text{ days}}^{t=14 \text{ days}} \left( B_{SS} \cdot SS_0(t) + B_{COD} \cdot COD_0(t) + B_{Nkj} \cdot S_{Nkj,0}(t) + B_{NO} \cdot S_{NO,0}(t) + B_{BOD5} \cdot BOD_0(t) \right) Q_0(t)$$

with:

$$S_{Nkj,0} = S_{NH,0} + S_{ND,0} + X_{ND,0} + i_{XB} (X_{B,H,0} + X_{X,A,0}) + i_{XP} (X_{P,0} + X_{I,0})$$

$$SS_0 = 0.75 \cdot (X_{S,0} + X_{I,0} + X_{B,H,0} + X_{B,A,0} + X_{P,0})$$

$$BOD_{5,0} = 0.65 \cdot (S_{S,0} + X_{S,0} + (1 - f_P) \cdot (X_{B,H,0} + X_{B,A,0}))$$
$$COD_0 = S_{S,0} + S_{I,0} + X_{S,0} + X_{I,0} + X_{B,H,0} + X_{B,A,0} + X_{P,0}$$

Finally an **Overall Cost Index (OCI)** is calculated:

$$OCI = AE + PE + 5 \cdot SP + 3 \cdot EC + ME$$

Tests of performance assessment, in open and closed-loop, can be found in Appendices 2 and 3 respectively.

## 7. Sensors and control handles

### 7.1. Introduction

To test your own control strategy on the benchmark plant appropriate sensors and actuators must be selected. To avoid unrealistic control behaviour, the dynamic behaviour of sensors and actuators (control handles) as well as additional measurement noise must be considered. To allow for a wide range of different strategies to be tested (within the confinement of the physical plant layout) a significant number of sensors and control handles are available. Their mathematical descriptions focus on simplicity rather than completely accurate reproductions of their true behaviour.

The principle for any good control strategy implies that the number of sensors and control actions should be minimised within the framework of the selected control strategy, due to the investment cost, maintenance cost, etc (Rieger *et al.*, 2003).

For initialisation purposes, first test of control concepts, or evaluation of the theoretical potential of control options it is of course a valid option to use ideal sensors (no noise, no delay). For internal flows (e.g. return sludge, internal recycle) which are basically control handles it can be assumed, that the flow rates are known or can be measured without errors and delays. For such an ideal sensor no specific sensor model is required. But the usage of ideal sensors should be reported.

### 7.2. Sensors

The aim of the sensor classification is to describe different sensor types but also to limit the number of sensor classes in order to ease the comparison of the simulation results. The benchmark deals with control strategies, therefore only a few related criteria are used and only one minimal measuring interval of 5 minutes is taken into account. It is not intended to define a user configurable class, since this would make it difficult to compare different benchmark studies. Should it nevertheless be impossible to choose a class, the benchmark model user is requested to describe the specific sensor in detail.

The main parameter to describe the sensor dynamics of the sensor classes is the “Response time”. This parameter is defined in an ISO norm (ISO 2003) and characterises the sensor dynamics based on a step response as presented in Figure 6.

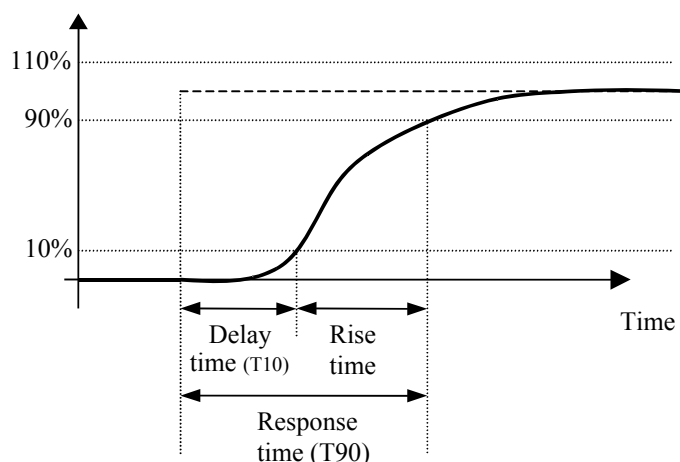


Figure 6: Definition of response time

In the norm the response time consists of the delay and the rise (fall) time. The (transport) delay time is defined as the time to reach 10% of the final value of a step response ( $T_{10}$ ). Thus the delay time in this context is not exactly the same as a transport delay time or dead-time defined in control engineering. The overall time to reach (and not to leave) a band from 90% - 110% of the final value of the step response is introduced as response time (here  $T_{90}$ ). To describe the dynamics of a sensor it is assumed that the two values delay time and response time (as defined by Figure 6) are given. For the definition of the benchmark sensor classes a response time ( $T_{90}$ ) is proposed.

The six sensor classes are shown in Table 11 and a list of typical sensors is provided in Table 12.

Sensor classes	Response time ( $T_{90}$ ) [min]	Measuring interval ( $T_0$ ) [min]	Examples
Class A	1	0	Ion sensitive, optical without filtration
Class B <sub>0</sub>	10	0	Gas sensitive + fast filtration
Class B <sub>1</sub>	10	5	Photometric + fast filtration
Class C <sub>0</sub>	20	0	Gas-sensitive + slow filtration
Class C <sub>1</sub>	20	5	Photometric + slow filtration or sedimentation
Class D	30	30	Photometric or titrimetric for total components

Table 11: Sensor classes

The response time includes the whole system with filtration unit and measuring system. Class A is a more or less ideal sensor; the response time of 1 minute is chosen in order to prevent unrealistic control applications. Class B contains mainly classical on-line analyzers with a fast filtration and short sample loops. In Class C analyzers with a slow filtration or sedimentation unit are described. Class D includes all batch measurements like respirometer and sensors for total components. To take into account continuously and discontinuously measuring sensors the classes B and C are divided into two subclasses. Five minutes is selected as the measuring interval, which is a typical minimum value for photometric analyzers. Longer intervals are not useful for control actions and are therefore neglected.

Additional to choosing the sensor class, the user has to define the measuring range for each sensor. Depending on the chosen measurement range the standard deviation is assumed to be 2.5% of the maximum measurement value (see sensor model description).

Real measurement signals always include measurement noise, which can lead to unwanted control actions or slow down the reaction. Therefore noise is included in the sensor model. The idea is not to model noise exactly, but to take into account some of its effects. In order to get comparable benchmark simulation results the noise signal is defined. Choice of a random signal would have required running each benchmark simulation a large number of times in order to eliminate the influence of the random signal. The noise signal is chosen with a standard deviation of 1, which is multiplied with the defined noise level (2.5% of the maximum measurement value). The noise is white zero-mean normally distributed noise. Other types of noise would be too specific and the sensors within one class would not be comparable.

As an example of how to use the sensor classes given in the table, the oxygen and nitrate sensors described for the default closed-loop test case can now very easily be described as:

- oxygen sensor: Class A, measurement range: 0-10 g (-COD).m<sup>-3</sup> and measurement noise  $\delta = 0.25$  g (-COD).m<sup>-3</sup>.
- nitrate sensor: Class B0 with a measurement range 0-20 g N.m<sup>-3</sup> and measurement noise  $\delta = 0.5$  g N.m<sup>-3</sup>.

### 7.3. Sensor model description

To ensure equal implementation and behaviour of the sensor models it is necessary to describe the model in detail. The following description is the result of a Simulink implementation and takes into account a number of performance issues which are similar for most of the simulation systems.

The proposed sensor classes contain a set of continuous (A, B<sub>0</sub>, C<sub>0</sub>) and time-discrete sensor models (B<sub>1</sub>, C<sub>1</sub>, D). Continuous models are preferred to time-discrete ones for implementing the continuous sensors for performance reasons. The discontinuous sensors B<sub>1</sub> and C<sub>1</sub> are modelled in a similar way but include an output sample and hold function. Sensor class D is modelled only in discrete form.

#### 7.3.1. Continuously measuring sensors

For the sensor classes A, B<sub>0</sub> and C<sub>0</sub> the approach is shown in Figure 7:

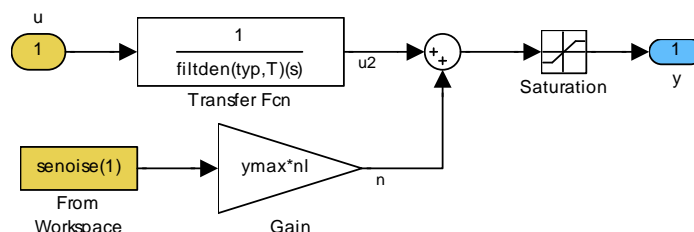


Figure 7: Simulink model of sensor lass A, B<sub>0</sub> and C<sub>0</sub>

Measured variable	Sensor types	Response time [min]	Measurement frequency [min]
MLSS [ $\text{g}\cdot\text{m}^{-3}$ ]	A	0	0
Turbidity [FNU or $\text{gTSS}\cdot\text{m}^{-3}$ ]	A		
$S_{\text{NH}_4}$ (ion sensitive)	A		
$S_{\text{NO}_x}$ (ion sensitive)	A		
$S_{\text{NO}_x}$ (UV)	A		
$C_{\text{COD}}, S_{\text{COD}}$ (UV/Vis)	A		
Flow rate [ $\text{m}^3\cdot\text{d}^{-1}$ ]	A		
Water level [m]	A		
Temperature [ $^{\circ}\text{C}$ ]	A		
pH	A		
$S_{\text{O}}$ [ $\text{g}(-\text{COD})\cdot\text{m}^{-3}$ ]	A		
Sludge blanket height [m]	A		
$S_{\text{NH}_4}$ (gas sensitive + normal filtration)	B <sub>0</sub>	10	0
$S_{\text{NO}_x}$ (UV + normal filtration)	B <sub>0</sub>		
$S_{\text{NH}_4}$ (photometric + normal filtration)	B <sub>1</sub>	10	5
$S_{\text{NO}_3}$ (photometric + normal filtration)	B <sub>1</sub>		
$S_{\text{NO}_2}$ (photometric + normal filtration)	B <sub>1</sub>		
$S_{\text{PO}_4}$ (photometric + normal filtration)	B <sub>1</sub>		
$S_{\text{NH}_4}$ (gassensitive + slow filtration or sedimentation)	C <sub>0</sub>	20	0
$S_{\text{NO}_x}$ (UV + slow filtration or sedimentation)	C <sub>0</sub>		
$S_{\text{NH}_4}$ (photometric + slow filtration or sedimentation)	C <sub>1</sub>	20	5
$S_{\text{NO}_3}$ (photometric + slow filtration or sedimentation)	C <sub>1</sub>		
$S_{\text{NO}_2}$ (photometric + slow filtration or sedimentation)	C <sub>1</sub>		
$S_{\text{PO}_4}$ (photometric + slow filtration or sedimentation)	C <sub>1</sub>		
$C_{\text{COD}}$ (thermal chemical oxidation + photometric)	D	30	30
TOC (thermal oxidation + IR detector)	D		
$C_{\text{N}}$ (thermal oxidation + IR detector or chemoluminescence detector)	D		
$C_{\text{P}}$ (thermal chemical oxidation + photometric)	D		
Respirometer	D		
Titration biosensor (alkalinity)	D		

Table 12: Typical sensor characteristics within the proposed classification scheme.

The original sensor signal  $u$  is transformed by a linear transfer function (block Transfer Fcn). This transfer function is used to implement the expected time response of the sensor. Real time behaviour of sensors is typically a combination of transport delay time behaviour (or dead time) caused by sample transport and preparation and a first or higher order dynamics (time constants) caused by different reasons, e.g. a mixing tank.



To have a sensor model with the same response time, a series of equal first order delay transfer functions is assumed. The number of first order transfer functions in series ( $n$ ) determines the ratio of delay time and response time (as defined in Figure 6). Table 13 shows the parameters for the response-time modelling (see specific sensor model) of the continuously operating sensors.

Sensor class	$T_{90}$	$n$	$T$	$R_{T10/T90}$
A	1 min	2	0.257	0.133
B <sub>0</sub>	10 min	8	0.849	0.392
C <sub>0</sub>	20 min	8	1.699	0.392

Table 13: Parameters for response time modelling.

For the sensor class A a response time ( $T_{90}$ ) of 1 min and a system order of  $n = 2$  is suggested. This results into a ratio of  $T_{10}$  (delay time) to  $T_{90}$  (response time)  $R_{T10/T90} = 0.133$ . Thus the transport delay is only a small fraction of the response time as typical for this sensor class. The assumed transfer function is finally

$$G_s(s) = \frac{1}{1+Ts} \frac{1}{1+Ts}$$

with  $T = T_{90} / 3.89$ .

For the sensor classes B and C a system order of  $n = 8$  is assumed. This will lead to a ratio of the delay time to the response time of  $R_{T10/T90} = 0.392$ . In this case the delay time is already approximately 40% of the response time. This is assumed to consider the significant effect of the transport of the sample for the sensor classes B and C. For class B a response time of 10 min and for class C of 20 min is selected. The assumed transfer function is finally

$$G_s(s) = \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts} \frac{1}{1+Ts}$$

with  $T = T_{90} / 11.7724$ .

The step responses for the classes A, B<sub>0</sub> and C<sub>0</sub> are presented in Figure 8.

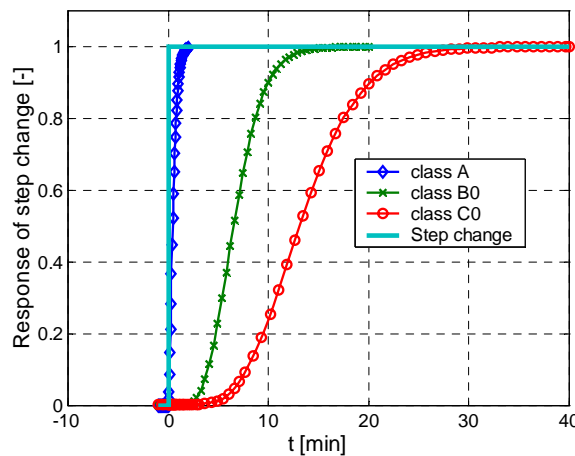


Figure 8: Step response of classes A, B<sub>0</sub>, C<sub>0</sub>.

The noise is modelled with a constant noise level  $nl$ . In the SIMULINK model presented in Figure 9 the noise signal (white noise with a standard deviation  $\delta=1$ ) is multiplied by the noise level  $nl$  and the maximum value of the measurement interval  $y_{max}$ . A normal distributed (standard deviation 1), frequency limited noise signal has been created and provided as an ASCII file (“sennoise.asc”) on the website (<http://www.benchmarkwwtp.org>) to allow the reproduction of results. The signal was created using a sample time of 1 min. The file must be interpolated using linear interpolation to provide a continuous noise signal. Using the sample time of 1 min together with the linear interpolation will limit the frequency spectrum of the noise (cut-of of high frequencies - pink noise). The file contains 25 columns of independent noise data for 14 days. For different sensors also different noise columns should be used to avoid correlated noise on different sensor signals.

In the Simulink model presented in Figure 7, the block 'From Workspace' will read the ASCII file using a linear interpolation. The noise signal is multiplied by the noise level  $nl$  and the maximum value of the measurement interval  $y_{max}$ . Thus the resulting noise signal will have a standard deviation of  $nl*y_{max}$ . The noise will be added to the delayed measurement signal ( $u_2$ ) and the resulting value will be limited to the measurement interval (0,  $y_{max}$ ). This is performed using the 'Saturation' block for the example implementation in Figure 7.

The noise is added to the delayed measurement signal and limited to the measurement interval (0,  $y_{max}$ ). The noise level is defined as  $nl = 0.025$  for all benchmark sensor classes (= 2.5% of the maximum measurement value).

### 7.3.2. Discontinuously measuring sensors

Sensor classes  $B_1$ ,  $C_1$  and D are operated discontinuously using a sample time  $T_0$ . An example of an implementation using a SIMULINK model is presented in Figure 9. The implementation is similar to that used in the model for the continuously measuring sensors but includes an additional output sample and hold function.

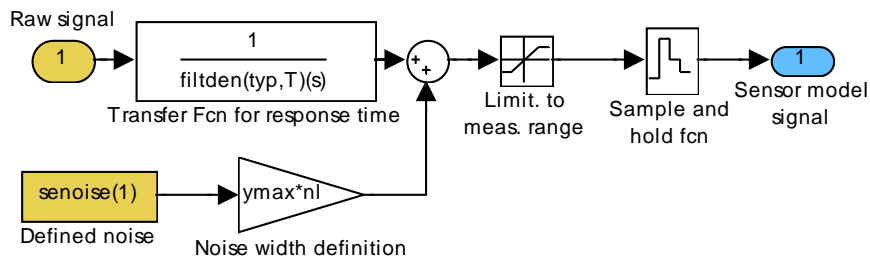


Figure 9: Simulink implementation class  $B_1$ ,  $C_1$ .

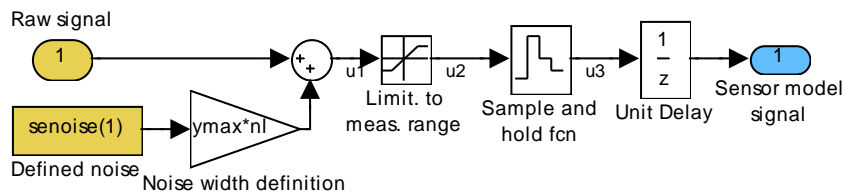


Figure 10: Simulink implementation class D.

Sensor class D represents batch-type reactors, for which any of the continuous delay times are negligible, compared to the batch operation of the measurement. An appropriate SIMULINK

implementation is demonstrated in Figure 10. This model adds noise to the original signal, limits the sum to the measuring range (0,  $y_{max}$ ) and uses a sample and hold function followed by a unit delay ( $y(k)=u3(k-1)$ ). Figure 11 shows examples of the output signal for all sensor classes.

### 7.3.3. Conclusions

Table 14 summarizes the recommended sensor parameter values for BSM1. Except for the plant influent flow rate, all the other flows are not explicitly measured but can be considered as known for simplicity.

## 7.4. Control handles

For reasons of simplicity all available control handles are considered to be ideal with regard to their behaviour. In the closed-loop test case only two control handles were used: the internal recirculation flow rate ( $Q_a$ ) and the oxygen transfer rate in reactor number 5 ( $K_{La5}$ ). The following control handles are considered to exist for the implementation of new control strategies on the benchmark plant:

- internal flow recirculation rate ( $Q_a$ );
- return sludge flow rate ( $Q_r$ );
- wastage flow rate ( $Q_w$ );
- anoxic/aerobic volume – all five biological reactors are equipped with both aerators and mechanical mixing devices, i.e. in a discrete fashion the volumes for anoxic and aerobic behaviour can be modified;
- aeration intensity individually for each reactor ( $K_{La1}, K_{La2}, K_{La3}, K_{La4}, K_{La5}$ );
- external carbon source flow rate ( $q_{EC1}, q_{EC2}, q_{EC3}, q_{EC4}, q_{EC5}$ ) where the carbon source is considered to consist of readily biodegradable substrate, i.e.  $COD_{EC}$ ;
- influent distribution by use of step feed (fractions of the influent flow to each of the five biological reactors:  $f_{Qinflow1}, f_{Qinflow2}, f_{Qinflow3}, f_{Qinflow4}, f_{Qinflow5}$ );
- distribution of internal flow recirculation (fractions of the internal recirculation flow to each of the five biological reactors:  $f_{Qa1}, f_{Qa2}, f_{Qa3}, f_{Qa4}, f_{Qa5}$ );
- distribution of return sludge flow (fractions of the return sludge flow to each of the five biological reactors:  $f_{Qr1}, f_{Qr2}, f_{Qr3}, f_{Qr4}, f_{Qr5}$ );

The above selection gives about 30 individual control handles with which to manipulate the defined benchmark plant and dramatically increases its flexibility. Such a number of available control handles may not be realistic for a real plant but is defined for the benchmark plant in order to allow for basically any type of general control strategy. This is after all the main purpose of the benchmark. The defined limitations for the different control handles are given in Table 15.

The aeration system ( $K_{La1}$ -  $K_{La5}$ ) is defined with significant dynamics. A response time of  $T_{90}=4$  min is considered (see Rieger *et al.*, 2005). A second order time delay function gives a reasonable model of this process. The time constant of each of the two identical first order delays is  $T = T_{90} / 3.89 = 1.03$  min.

Measured variable	Class	Measurement Range	Measurement noise ( $\delta$ )
Flow rate ( $\text{m}^3 \cdot \text{d}^{-1}$ ) high range	A	0-100 000	2500
Water level (m)	A	0-5	0.125
Temperature ( $^{\circ}\text{C}$ )	A	5-25	0.5
pH	A	5-9	0.1
$S_O$ ( $\text{g (-COD)} \cdot \text{m}^{-3}$ )	A	0-10	0.25
Sludge blanket level (m)	A	0-5	0.125
$S_{NO}$ ( $\text{g N} \cdot \text{m}^{-3}$ )	$B_0$	0-20	0.5
$S_{NH}$ ( $\text{g N} \cdot \text{m}^{-3}$ ) low range	$B_0$	0-20	0.5
$S_{NH}$ ( $\text{g N} \cdot \text{m}^{-3}$ ) high range	$B_0$	0-50	1.25
$S_{ALK}$ ( $\text{mol HCO}_3 \cdot \text{m}^{-3}$ )	$B_0$	0-20	0.5
Mixed-liquor suspended solids ( $\text{g} \cdot \text{m}^{-3}$ )	A	0-10 000	250
Effluent total suspended solids ( $\text{g} \cdot \text{m}^{-3}$ )	A	0-200	5
$\text{COD}_t$ ( $\text{g COD} \cdot \text{m}^{-3}$ )	D	0-1 000	25
OUR ( $\text{g (-COD)} \cdot \text{m}^{-3} \cdot \text{d}^{-1}$ )	D	0-2 000	50

Table 14: Recommended BSM1 sensor parameters.

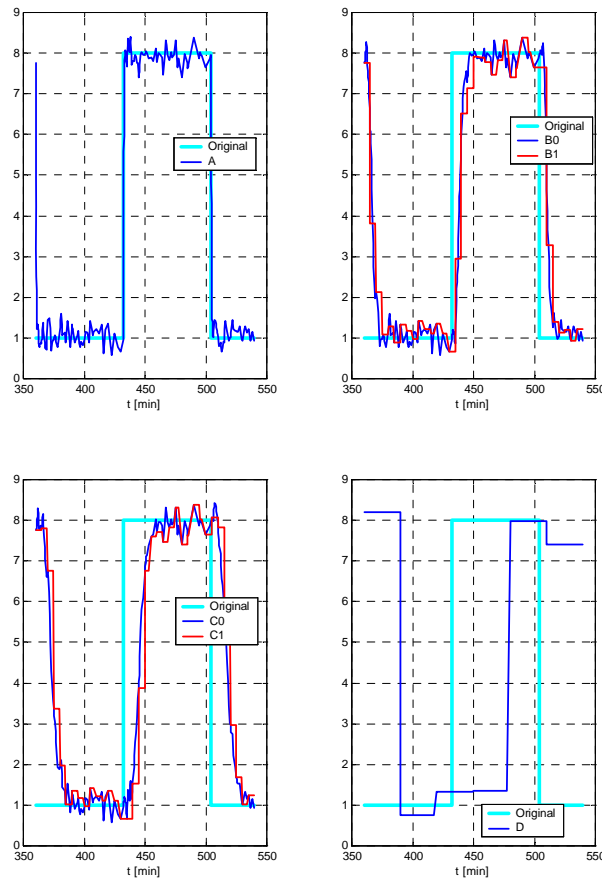


Figure 11: Pulse response of sensor classes.

### 7.5. Alternative description

To clarify the sensor and actuator models, a presentation in form of differential and difference equations is also presented in this section. The notations are summarized in Table 16.

#### 7.5.1 Model for sensor class A and actuator model

$$\frac{d x_1(t)}{dt} = \frac{1}{T} u(t) - \frac{1}{T} x_1(t)$$

$$\frac{d u_2(t)}{dt} = \frac{1}{T} x_1(t) - \frac{1}{T} u_2(t)$$

$$y_1(t) = u_2(t) + y_{\max} nl n(t)$$

$$y(t) = \begin{cases} y_1(t) > y_{\max} : y_{\max} \\ y_{\min} \leq y_1(t) \leq y_{\max} : y_1(t) \\ y_1(t) < y_{\min} : y_{\min} \end{cases}$$

#### 7.5.2. Model for sensor class B<sub>0</sub> and C<sub>0</sub>

$$\frac{d x_1(t)}{dt} = \frac{1}{T} u(t) - \frac{1}{T} x_1(t)$$

$$\frac{d x_{i+1}(t)}{dt} = \frac{1}{T} x_i(t) - \frac{1}{T} x_{i+1}(t); \quad i = 1:6$$

$$\frac{d u_2(t)}{dt} = \frac{1}{T} x_7(t) - \frac{1}{T} u_2(t)$$

$$y_1(t) = u_2(t) + y_{\max} nl n(t)$$

$$y(t) = \begin{cases} y_1(t) > y_{\max} : y_{\max} \\ y_{\min} \leq y_1(t) \leq y_{\max} : y_1(t) \\ y_1(t) < y_{\min} : y_{\min} \end{cases}$$

Control handle	Minimum value	Maximum value	Comments
$Q_a$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	92230	Max = 500% of $Q_{0,\text{stab}}$
$Q_r$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	36892	Max = 200% of $Q_{0,\text{stab}}$
$Q_w$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	1844.6	Max = 10% of $Q_{0,\text{stab}}$
$K_L a_1$ ( $\text{d}^{-1}$ )	0	360	Reactor 1
$K_L a_2$ ( $\text{d}^{-1}$ )	0	360	Reactor 2
$K_L a_3$ ( $\text{d}^{-1}$ )	0	360	Reactor 3
$K_L a_4$ ( $\text{d}^{-1}$ )	0	360	Reactor 4
$K_L a_5$ ( $\text{d}^{-1}$ )	0	360	Reactor 5
$q_{EC1}$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	5	Reactor 1 Carbon source conc. 400,000 g COD. $\text{m}^{-3}$ available as $COD_S$ (e.g. 25% ethanol solution)
$q_{EC2}$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	5	Reactor 2 Otherwise same as above
$q_{EC3}$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	5	Reactor 3 Otherwise same as above
$q_{EC4}$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	5	Reactor 4 Otherwise same as above
$q_{EC5}$ ( $\text{m}^3 \cdot \text{d}^{-1}$ )	0	5	Reactor 5 Otherwise same as above
$f_{Q_{in1}}, f_{Q_{in2}}, f_{Q_{in3}}, f_{Q_{in4}}, f_{Q_{in5}}$	0	1	Part of the influent flow rate distributed to each biological reactor Note: the sum of all five must always equal one
$f_{Q_{a1}}, f_{Q_{a2}}, f_{Q_{a3}}, f_{Q_{a4}}, f_{Q_{a5}}$	0	1	Part of the internal recirculation flow rate distributed to each biological reactor Note: the sum of all five must always equal one
$f_{Q_{r1}}, f_{Q_{r2}}, f_{Q_{r3}}, f_{Q_{r4}}, f_{Q_{r5}}$	0	1	Part of the sludge return flow rate distributed to each biological reactor Note: the sum of all five must always equal one

Table 15: Available control handles and their limitations.

$u(t)$	ideal measurement signal from process
$x_1(t) \dots x_7(t)$	internal states for dynamic part of sensor model
$u_2(t)$	delayed measurement signal (intermediate variable)
$y_1(t), y_2(t), y_3(k), y_4(k)$	intermediate signals
$y(t)$	real measurement signal from sensor (delayed, noisy, limited)
$T$	Time constant for one first order time delay
$T_0$	sample time for discontinuous sensor models

Table 16: Variables used in the sensor models

### 7.5.3. Model for sensor class $B_1$ and $C_1$

$$\frac{d x_1(t)}{dt} = \frac{1}{T} u(t) - \frac{1}{T} x_1(t)$$

$$\frac{d x_{i+1}(t)}{dt} = \frac{1}{T} x_i(t) - \frac{1}{T} x_{i+1}(t); \quad i = 1:6$$

$$\frac{d u_2(t)}{dt} = \frac{1}{T} x_7(t) - \frac{1}{T} u_2(t)$$

$$y_1(t) = u_2(t) + y_{\max} nl n(t)$$

$$y_2(t) = \begin{cases} y_1(t) > y_{\max} : y_{\max} \\ y_{\min} \leq y_1(t) \leq y_{\max} : y_1(t) \\ y_1(t) < y_{\min} : y_{\min} \end{cases}$$

$$y_3(k) = y_2(t, t = k * T_0)$$

$$y(t) = y_3(k, k = \text{floor}(t/T_0))$$

#### 7.5.4. Model for sensor D

$$y_1(t) = u(t) + y_{\max} nl n(t)$$

$$y_2(t) = \begin{cases} y_1(t) > y_{\max} : y_{\max} \\ y_{\min} \leq y_1(t) \leq y_{\max} : y_1(t) \\ y_1(t) < y_{\min} : y_{\min} \end{cases}$$

$$y_3(k) = y_2(t, t = k * T_0)$$

$$y_4(k) = y_3(k-1)$$

$$y(t) = y_4(k, k = \text{floor}(t/T_0))$$

## 8. Conclusions

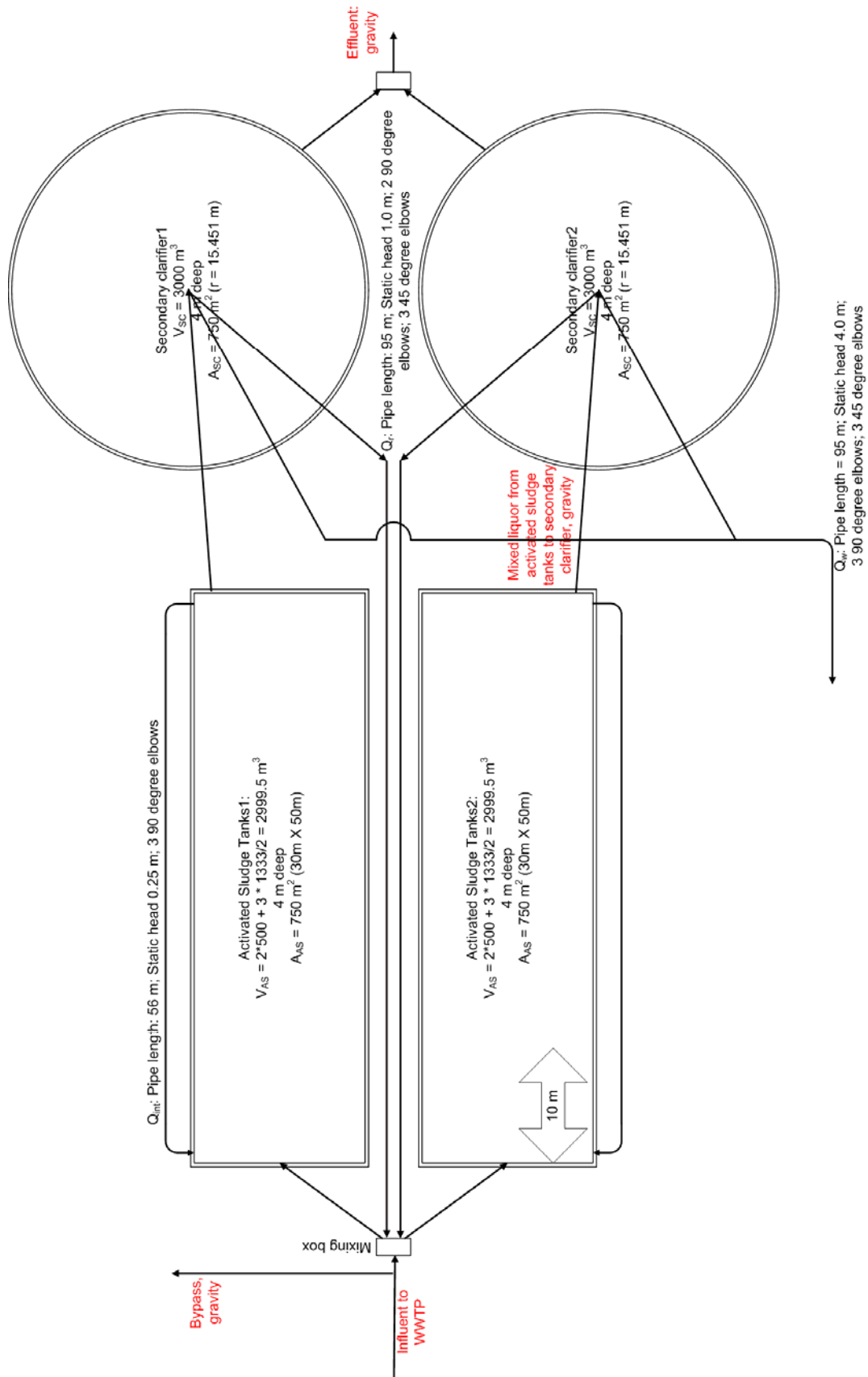
The document has described in details the implementation of BSM1. To further help the user, appendices 2 to 5 contains open-loop and closed-loop results obtained with a Matlab-Simulink and a FORTRAN implementations.

## 9. References

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### Appendix 1: Practical BSM1 plant layout



**Appendix 2: Open-loop performance (summary)**

Effluent average concentrations based on load		
Variable	Unit	FORTTRAN
Effluent average flow rate	$\text{m}^3 \cdot \text{d}$	18055.2
Effluent average $S_I$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	30.
Effluent average $S_S$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	0.9725
Effluent average $X_I$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	4.58
Effluent average $X_S$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	0.2231
Effluent average $X_{BH}$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	10.22
Effluent average $X_{BA}$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	0.5421
Effluent average $X_P$ concentration	$\text{g COD} \cdot \text{m}^{-3}$	1.757
Effluent average $S_O$ concentration	$\text{g (-COD)} \cdot \text{m}^{-3}$	0.7462
Effluent average $S_{NO}$ concentration	$\text{g N} \cdot \text{m}^{-3}$	8.801
Effluent average $S_{NH}$ concentration (limit = $4 \text{ g N} \cdot \text{m}^{-3}$ )	$\text{g N} \cdot \text{m}^{-3}$	4.794
Effluent average $S_{ND}$ concentration	$\text{g N} \cdot \text{m}^{-3}$	0.7308
Effluent average $X_{ND}$ concentration	$\text{g N} \cdot \text{m}^{-3}$	0.01571
Effluent average $S_{ALK}$ concentration	$\text{mol HCO}_3^- \cdot \text{m}^{-3}$	4.46
Effluent average $TSS$ concentration (limit = $30 \text{ g SS} \cdot \text{m}^{-3}$ )	$\text{g SS} \cdot \text{m}^{-3}$	12.99
Effluent average Kjeldahl N concentration	$\text{g N} \cdot \text{m}^{-3}$	6.782
Effluent average total N concentration (limit = $18 \text{ g N} \cdot \text{m}^{-3}$ )	$\text{g N} \cdot \text{m}^{-3}$	15.58
Effluent average total COD concentration (limit = $100 \text{ g COD} \cdot \text{m}^{-3}$ )	$\text{g COD} \cdot \text{m}^{-3}$	48.30
Effluent average $BOD_5$ concentration (limit = $10 \text{ g} \cdot \text{m}^{-3}$ )	$\text{g} \cdot \text{m}^{-3}$	2.775

Effluent average load		
Variable	Unit	FORTTRAN
Effluent average $S_I$ load	$\text{kg COD} \cdot \text{d}^{-1}$	541.656
Effluent average $S_S$ load	$\text{kg COD} \cdot \text{d}^{-1}$	17.558682
Effluent average $X_I$ load	$\text{kg COD} \cdot \text{d}^{-1}$	82.692816
Effluent average $X_S$ load	$\text{kg COD} \cdot \text{d}^{-1}$	4.02811512
Effluent average $X_{BH}$ load	$\text{kg COD} \cdot \text{d}^{-1}$	184.524144
Effluent average $X_{BA}$ load	$\text{kg COD} \cdot \text{d}^{-1}$	9.78772392
Effluent average $X_P$ load	$\text{kg COD} \cdot \text{d}^{-1}$	31.7229864
Effluent average $S_O$ load	$\text{kg (-COD)} \cdot \text{d}^{-1}$	13.47279024
Effluent average $S_{NO}$ load	$\text{kg N} \cdot \text{d}^{-1}$	158.9038152
Effluent average $S_{NH}$ load	$\text{kg N} \cdot \text{d}^{-1}$	86.5566288
Effluent average $y$ load	$\text{kg N} \cdot \text{d}^{-1}$	13.19474016
Effluent average $X_{ND}$ load	$\text{kg N} \cdot \text{d}^{-1}$	0.283647192
Effluent average $S_{ALK}$ load	$\text{kmol HCO}_3^- \cdot \text{d}^{-1}$	80.526192
Effluent average $TSS$ load	$\text{kg} \cdot \text{d}^{-1}$	234.537048
Effluent average Kjeldahl N load	$\text{kg N} \cdot \text{d}^{-1}$	122.4503664
Effluent average total N load	$\text{kg N} \cdot \text{d}^{-1}$	281.300016
Effluent average total COD load	$\text{kg COD} \cdot \text{d}^{-1}$	872.06616
Effluent average $BOD_5$ load	$\text{kg} \cdot \text{d}^{-1}$	50.10318

Effluent violations		
Variable	Unit	Value (FORTRAN)
95% percentile of effluent $S_{NH}$ ( $S_{NH,e95}$ ), updated BSM1	$\text{g N.m}^{-3}$	8.9175
95% percentile of effluent total N ( $N_{tot,e95}$ ), updated BSM1	$\text{g N.m}^{-3}$	18.535
95% percentile of effluent TSS ( $TSS_{e95}$ ), updated BSM1	$\text{g COD.m}^{-3}$	15.8
Maximum effluent total N limit ( $18 \text{ g N.m}^{-3}$ ) was violated		
during:	d	0.5761
% of total evaluation time:	%	8.23
number of violations:		5
Maximum effluent total COD limit ( $100 \text{ g COD.m}^{-3}$ ) was violated		
during:	d	0
% of total evaluation time:	%	0
number of violations:		0
Maximum effluent total ammonia limit ( $4 \text{ g N.m}^{-3}$ ) was violated		
during:	d	4.403
% of total evaluation time:	%	62.9
number of violations:		7
Maximum effluent total TSS limit ( $30 \text{ g SS.m}^{-3}$ ) was violated		
during:	d	0
% of total evaluation time:	%	0
number of violations:		0
Maximum effluent total BOD <sub>5</sub> limit ( $10 \text{ g.m}^{-3}$ ) was violated		
during:	d	0
% of total evaluation time:	%	0
number of violations:		0

Other output quality variables		
Variable	Unit	Value (FORTRAN)
Influent quality (IQ) index	kg poll.units.d <sup>-1</sup>	52100
Effluent quality (EQ) index	kg poll.units.d <sup>-1</sup>	6700
Sludge production for disposal	kg SS	17052
Average sludge production for disposal per day	kg SS.d <sup>-1</sup>	2436
Sludge production released into effluent	kg SS	1631
Average sludge production released into effluent per day	kg SS.d <sup>-1</sup>	233
Total sludge production	kg SS	18683
Total average sludge production per day	kg SS.d <sup>-1</sup>	2669

'Energy' related variables		
Variable	Unit	Value (FORTRAN)
Average aeration energy	kWh.d <sup>-1</sup>	3341
Average pumping energy	kWh.d <sup>-1</sup>	388.2
Average carbon source dosage	kg COD.d <sup>-1</sup>	0
Average mixing energy	kWh.d <sup>-1</sup>	240

Operational cost index		
Variable	Unit	Value (FORTRAN)
Sludge production cost index	-	12180
Aeration energy cost index	-	3341
Pumping energy cost index	-	388.2
Carbon source dosage cost index	-	0
Mixing energy cost index	-	240
Total Operational Cost Index (OCI)	-	16150

**Appendix 3: Closed-loop performance (summary)**

Effluent violations		
Variable	Unit	Value (MATLAB)
95% percentile of effluent $S_{NH}$ ( $S_{NH,e95}$ ), updated BSM1	$\text{g N.m}^{-3}$	7.3902
95% percentile of effluent total N ( $N_{tot,e95}$ ), updated BSM1	$\text{g N.m}^{-3}$	20.2693
95% percentile of effluent TSS ( $TSS_{e95}$ ), updated BSM1	$\text{g COD.m}^{-3}$	15.7663
Maximum effluent total N limit ( $18 \text{ g N.m}^{-3}$ ) was violated		
during:	d	1.2813
% of total evaluation time:	%	18.3036
number of violations:		7
Maximum effluent total COD limit ( $100 \text{ g COD.m}^{-3}$ ) was violated		
during:	d	0
% of total evaluation time:	%	0
number of violations:		0
Maximum effluent total ammonia limit ( $4 \text{ g N.m}^{-3}$ ) was violated		
during:	d	1.1979
% of total evaluation time:	%	17.1131
number of violations:		5
Maximum effluent total TSS limit ( $30 \text{ g SS.m}^{-3}$ ) was violated		
during:	d	0
% of total evaluation time:	%	0
number of violations:		0
Maximum effluent total BOD <sub>5</sub> limit ( $10 \text{ g.m}^{-3}$ ) was violated		
during:	d	0
% of total evaluation time:	%	0
number of violations:		0

Other output quality variables		
Variable	Unit	Value (MATLAB)
Influent quality (IQ) index	kg poll.units.d <sup>-1</sup>	52081.3952
Effluent quality (EQ) index	kg poll.units.d <sup>-1</sup>	6123.0182
Sludge production for disposal	kg SS	17084.2397
Average sludge production for disposal per day	kg SS.d <sup>-1</sup>	2440.6057
Sludge production released into effluent	kg SS	1643.7439
Average sludge production released into effluent per day	kg SS.d <sup>-1</sup>	234.8206
Total sludge production	kg SS	18727.9836
Total average sludge production per day	kg SS.d <sup>-1</sup>	2675.4262

'Energy' related variables		
Variable	Unit	Value (MATLAB)
Average aeration energy	kWh.d <sup>-1</sup>	3698.3438
Average pumping energy	kWh.d <sup>-1</sup>	241.0305
Average carbon source dosage	kg COD.d <sup>-1</sup>	0
Average mixing energy	kWh.d <sup>-1</sup>	240

Operational cost index		
Variable	Unit	Value (MATLAB)
Sludge production cost index	-	12203.0284
Aeration energy cost index	-	3698.3438
Pumping energy cost index	-	241.0305
Carbon source dosage cost index	-	0
Mixing energy cost index	-	240
Total Operational Cost Index (OCI)	-	16382.4027

Controller performance		
Nitrate controller		
	Unit	Value (MATLAB)
Controller type		continuous PI with K=10000 $\text{m}^3 \cdot \text{d}^{-1} \cdot (\text{g N} \cdot \text{m}^{-3})^{-1}$ , Ti=0.025 d, Tt=1.015 d
Set point $S_{NO,2}$	$\text{g N} \cdot \text{m}^{-3}$	1
Average of $e_{NO3}$	$\text{g N} \cdot \text{m}^{-3}$	-0.0021211
Average of $ e_{NO3} $	$\text{g N} \cdot \text{m}^{-3}$	0.20497
IAE $e_{NO3}$	$\text{g N} \cdot \text{m}^{-3} \cdot \text{d}$	1.4348
ISE $e_{NO3}$	$(\text{g N} \cdot \text{m}^{-3})^2 \cdot \text{d}$	0.56897
Max $e_{NO3}$	$\text{g N} \cdot \text{m}^{-3}$	0.91782
Standard deviation of $e_{NO3}$	$\text{g N} \cdot \text{m}^{-3}$	0.28509
Variance of $e_{NO3}$	$(\text{g N} \cdot \text{m}^{-3})^2$	0.081276
Max deviation of $Q_a$	$\text{m}^3 \cdot \text{d}^{-1}$	45734.3965
Max deviation of $Q_a$ in 1 sample	$\text{m}^3 \cdot \text{d}^{-1}$	18918.9397
Average value of $Q_a$	$\text{m}^3 \cdot \text{d}^{-1}$	18610.0823
Standard deviation of $Q_a$	$\text{m}^3 \cdot \text{d}^{-1}$	4078.4756
Variance of $Q_a$	$(\text{m}^3 \cdot \text{d}^{-1})^2$	16633963.24

Controller performance		
Dissolved oxygen controller		
	Unit	Value (MATLAB)
Controller type		continuous PI with antiwindup, K=25 $\text{d}^{-1} \cdot (\text{g (-COD)} \cdot \text{m}^{-3})^{-1}$ , Ti=0.002 d, Tt=0.001 d
Set point $S_{O,5}$	$\text{g (-COD)} \cdot \text{m}^{-3}$	2
Average of $e_{SO5}$	$\text{g (-COD)} \cdot \text{m}^{-3}$	-0.00039763
Average of $ e_{SO5} $	$\text{g (-COD)} \cdot \text{m}^{-3}$	0.084044
IAE $e_{SO5}$	$\text{g (-COD)} \cdot \text{m}^{-3} \cdot \text{d}$	0.58831
ISE $e_{SO5}$	$(\text{g (-COD)} \cdot \text{m}^{-3})^2 \cdot \text{d}$	0.083975
Max $e_{SO5}$	$\text{g (-COD)} \cdot \text{m}^{-3}$	0.39631
Standard deviation of $e_{SO5}$	$\text{g (-COD)} \cdot \text{m}^{-3}$	0.10953
Variance of $e_{SO5}$	$(\text{g (-COD)} \cdot \text{m}^{-3})^2$	0.011996
Max deviation of $K_{LA5}$	$\text{d}^{-1}$	242.2831
Max deviation of $K_{LA5}$ in 1 sample	$\text{d}^{-1}$	47;8828
Average value of $K_{LA5}$	$\text{d}^{-1}$	144.1219
Standard deviation of $K_{LA5}$	$\text{d}^{-1}$	9.5682
Variance of $K_{LA5}$	$(\text{d}^{-1})^2$	91.5507

**STEADY STATE RESULTS FOR OPENLOOP**

**(Results from Matlab/Simulink implementation by Dr Ulf Jeppsson, IEA, Lund University, Sweden, March 27 2008)**

## Influent characteristics

\*\*\*\*\*  
 SI = 30 mg COD/l  
 SS = 69.5 mg COD/l  
 XI = 51.2 mg COD/l  
 XS = 202.32 mg COD/l  
 XBH = 28.17 mg COD/l  
 XBA = 0 mg COD/l  
 XP = 0 mg COD/l  
 SO = 0 mg -COD/l  
 SNO = 0 mg N/l  
 SNH = 31.56 mg N/l  
 SND = 6.95 mg N/l  
 XND = 10.59 mg N/l  
 SALK = 7 mol HCO<sub>3</sub>/m<sup>3</sup>  
 TSS = 211.2675 mg SS/l

## Flow conditions

\*\*\*\*\*  
 Influent flow to WWTP = 18446 m<sup>3</sup>/d  
 Influent flow to AS = 92230 m<sup>3</sup>/d  
 Internal recirculation = 55338 m<sup>3</sup>/d  
 Settler feed flow = 36892 m<sup>3</sup>/d  
 Returned sludge flow = 18446 m<sup>3</sup>/d  
 Wastage sludge flow = 385 m<sup>3</sup>/d  
 Effluent flow = 18061 m<sup>3</sup>/d

## Input to AS

\*\*\*\*\*  
 SI = 30 mg COD/l  
 SS = 14.6116 mg COD/l  
 XI = 1149.1183 mg COD/l  
 XS = 89.3302 mg COD/l  
 XBH = 2542.1684 mg COD/l  
 XBA = 148.4614 mg COD/l  
 XP = 448.1754 mg COD/l  
 SO = 0.39275 mg -COD/l  
 SNO = 8.3321 mg N/l  
 SNH = 7.6987 mg N/l  
 SND = 1.9406 mg N/l  
 XND = 5.6137 mg N/l  
 SALK = 4.7005 mol HCO<sub>3</sub>/m<sup>3</sup>  
 TSS = 3282.9402 mg SS/l

## Reactor 1

\*\*\*\*\*  
 SI = 30 mg COD/l  
 SS = 2.8082 mg COD/l  
 XI = 1149.1183 mg COD/l  
 XS = 82.1349 mg COD/l  
 XBH = 2551.7631 mg COD/l  
 XBA = 148.3886 mg COD/l  
 XP = 448.8459 mg COD/l  
 SO = 0.0042984 mg -COD/l  
 SNO = 5.3699 mg N/l  
 SNH = 7.9179 mg N/l  
 SND = 1.2166 mg N/l  
 XND = 5.2849 mg N/l  
 SALK = 4.9277 mol HCO<sub>3</sub>/m<sup>3</sup>



TSS = 3285.188 mg SS/l

Reactor 2

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 1.4588 mg COD/l  
XI = 1149.1182 mg COD/l  
XS = 76.3862 mg COD/l  
XBH = 2553.3824 mg COD/l  
XBA = 148.3083 mg COD/l  
XP = 449.5167 mg COD/l  
SO = 6.3132e-05 mg -COD/l  
SNO = 3.6619 mg N/l  
SNH = 8.3445 mg N/l  
SND = 0.88207 mg N/l  
XND = 5.0291 mg N/l  
SALK = 5.0802 mol HCO<sub>3</sub>/m<sup>3</sup>  
TSS = 3282.5339 mg SS/l

Reactor 3

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 1.1495 mg COD/l  
XI = 1149.1182 mg COD/l  
XS = 64.8549 mg COD/l  
XBH = 2557.1288 mg COD/l  
XBA = 148.9404 mg COD/l  
XP = 450.4123 mg COD/l  
SO = 1.7184 mg -COD/l  
SNO = 6.5408 mg N/l  
SNH = 5.548 mg N/l  
SND = 0.82889 mg N/l  
XND = 4.3924 mg N/l  
SALK = 4.6748 mol HCO<sub>3</sub>/m<sup>3</sup>  
TSS = 3277.841 mg SS/l

Reactor 4

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.99532 mg COD/l  
XI = 1149.1182 mg COD/l  
XS = 55.694 mg COD/l  
XBH = 2559.18 mg COD/l  
XBA = 149.5262 mg COD/l  
XP = 451.3087 mg COD/l  
SO = 2.4289 mg -COD/l  
SNO = 9.299 mg N/l  
SNH = 2.9674 mg N/l  
SND = 0.76679 mg N/l  
XND = 3.879 mg N/l  
SALK = 4.2935 mol HCO<sub>3</sub>/m<sup>3</sup>  
TSS = 3273.6203 mg SS/l

Reactor 5

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.88949 mg COD/l  
XI = 1149.1182 mg COD/l  
XS = 49.3056 mg COD/l  
XBH = 2559.341 mg COD/l  
XBA = 149.7963 mg COD/l  
XP = 452.2051 mg COD/l  
SO = 0.49094 mg -COD/l

SNO = 10.4152 mg N/l  
SNH = 1.7334 mg N/l  
SND = 0.68828 mg N/l  
XND = 3.5272 mg N/l  
SALK = 4.1256 mol HCO3/m3  
TSS = 3269.8246 mg SS/l

Settler underflow

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.88949 mg COD/l  
XI = 2247.0367 mg COD/l  
XS = 96.4143 mg COD/l  
XBH = 5004.6489 mg COD/l  
XBA = 292.9183 mg COD/l  
XP = 884.2618 mg COD/l  
SO = 0.49094 mg -COD/l  
SNO = 10.4152 mg N/l  
SNH = 1.7334 mg N/l  
SND = 0.68828 mg N/l  
XND = 6.8972 mg N/l  
SALK = 4.1256 mol HCO3/m3  
TSS = 6393.9599 mg SS/l

Settler effluent

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.88949 mg COD/l  
XI = 4.3918 mg COD/l  
XS = 0.18844 mg COD/l  
XBH = 9.7815 mg COD/l  
XBA = 0.57251 mg COD/l  
XP = 1.7283 mg COD/l  
SO = 0.49094 mg -COD/l  
SNO = 10.4152 mg N/l  
SNH = 1.7334 mg N/l  
SND = 0.68828 mg N/l  
XND = 0.01348 mg N/l  
SALK = 4.1256 mol HCO3/m3  
TSS = 12.4969 mg SS/l

Settler internal (1 is top layer)

\*\*\*\*\*

TSS1 = 12.4969 mg SS/l  
TSS2 = 18.1132 mg SS/l  
TSS3 = 29.5402 mg SS/l  
TSS4 = 68.9779 mg SS/l  
TSS5 = 356.0738 mg SS/l  
TSS6 = 356.0738 mg SS/l  
TSS7 = 356.0738 mg SS/l  
TSS8 = 356.0738 mg SS/l  
TSS9 = 356.0738 mg SS/l  
TSS10 = 6393.9599 mg SS/l

Other variables

\*\*\*\*\*

Trad. sludge age (XS + XP + XI + XBH + XBA in reactors) = 7.3155 days  
Spec. sludge age (XBH + XBA in reactors and settler) = 9.1436 days  
Total hydraulic retention time = 15.6118 hours  
Reactor hydraulic retention time = 7.8053 hours  
Thickening factor at bottom of settler (TSSu/TSSfeed) = 1.9554  
Thinning factor at top of settler (TSSeff/TSSfeed) = 0.0038219

## Dimensions

\*\*\*\*\*

Reactor 1 is anoxic  
Volume reactor 1 = 1000 m3  
Reactor 2 is anoxic  
Volume reactor 2 = 1000 m3  
Reactor 3 is aerobic  
Volume reactor 3 = 1333 m3  
Reactor 4 is aerobic  
Volume reactor 4 = 1333 m3  
Reactor 5 is aerobic  
Volume reactor 5 = 1333 m3  
Settler height = 4 m  
Settler area = 1500 m2  
Settler volume = 6000 m3

## DYNAMIC RESULTS FOR OPENLOOP

(Results from Matlab/Simulink implementation by Dr Ulf Jeppsson, IEA, Lund University, Sweden, March 27 2008)

### SUMMARY OF PLANT PERFORMANCE

\*\*\*\*\*

The plant was simulated in openloop for 150 days to achieve steady state using the CONSTANTINPUT file.

Then the DRYWEATHER file was used to simulate the dynamics during 14 days and set up the plant for the dynamic simulations.

The results of this simulation was used as initial values for the actual plant performance calculations using the different dynamic input files.

\*\*\*\*\*

\* DRYWEATHER FILE \*

\*\*\*\*\*

Overall plant performance during time 7 to 14 days

\*\*\*\*\*

Effluent average concentrations based on load

-----  
Effluent average flow rate = 18061.3325 m3/d  
Effluent average SI conc = 30 mg COD/l  
Effluent average SS conc = 0.97352 mg COD/l  
Effluent average XI conc = 4.5794 mg COD/l  
Effluent average XS conc = 0.22285 mg COD/l  
Effluent average XBH conc = 10.2208 mg COD/l  
Effluent average XBA conc = 0.54217 mg COD/l  
Effluent average XP conc = 1.7572 mg COD/l  
Effluent average SO conc = 0.74639 mg (-COD)/l  
Effluent average SNO conc = 8.8238 mg N/l  
Effluent average SNH conc = 4.7589 mg N/l (limit = 4 mg N/l)  
Effluent average SND conc = 0.72901 mg N/l  
Effluent average XND conc = 0.015691 mg N/l  
Effluent average SALK conc = 4.4562 mol HCO3/m3  
Effluent average TSS conc = 12.9917 mg SS/l (limit = 30 mg SS/l)

Effluent average Kjeldahl N conc = 6.7448 mg N/l  
Effluent average total N conc = 15.5686 mg N/l (limit = 18 mg COD/l)  
Effluent average total COD conc = 48.2958 mg COD/l (limit = 100 mg COD/l)  
Effluent average BOD5 conc = 2.7746 mg/l (limit = 10 mg/l)

Effluent average load

-----  
Effluent average SI load = 541.84 kg COD/day  
Effluent average SS load = 17.583 kg COD/day  
Effluent average XI load = 82.7093 kg COD/day  
Effluent average XS load = 4.025 kg COD/day  
Effluent average XBH load = 184.6007 kg COD/day  
Effluent average XBA load = 9.7924 kg COD/day  
Effluent average XP load = 31.7368 kg COD/day  
Effluent average SO load = 13.4807 kg (-COD)/day  
Effluent average SNO load = 159.3704 kg N/day  
Effluent average SNH load = 85.9513 kg N/day  
Effluent average SND load = 13.1668 kg N/day  
Effluent average XND load = 0.28341 kg N/day  
Effluent average SALK load = 80.4845 kmol HCO3/day  
Effluent average TSS load = 234.6482 kg SS/day

Effluent average Kjeldahl N load = 121.8198 kg N/d  
Effluent average total N load = 281.1902 kg N/d

Effluent average total COD load = 872.2873 kg COD/d  
Effluent average BOD5 load = 50.1124 kg/d

#### Other effluent quality variables

-----  
Influent Quality (I.Q.) index = 52081.3952 kg poll.units/d  
Effluent Quality (E.Q.) index = 6690.1066 kg poll.units/d

Sludge production for disposal = 17049.8309 kg SS  
Average sludge production for disposal per day = 2435.6901 kg SS/d  
Sludge production released into effluent = 1642.5375 kg SS  
Average sludge production released into effluent per day = 234.6482 kg SS/d  
Total sludge production = 18692.3684 kg SS  
Total average sludge production per day = 2670.3383 kg SS/d

Total aeration energy = 23389.7067 kWh  
Average aeration energy per day = 3341.3867 kWh/d

Total pumping energy (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 2717.19 kWh  
Average pumping energy per day (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 388.17 kWh/d

Total mixing energy = 1680 kWh  
Average mixing energy per day = 240 kWh/d

Total added carbon volume = 0 m<sup>3</sup>  
Average added carbon flow rate = 0 m<sup>3</sup>/d  
Total added carbon mass = 0 kg COD  
Average added carbon mass per day = 0 kg COD/d

#### Operational Cost Index

-----  
Aeration energy cost index = 3341.3867  
Pumping energy cost index = 388.17  
Carbon source addition cost index = 0  
Mixing energy cost index = 240  
Total Operational Cost Index (OCI) = 16148.0073

#### Effluent violations

-----  
95% percentile for effluent SNH (Ammonia<sub>95</sub>) = 8.8818 g N/m<sup>3</sup>  
95% percentile for effluent TN (TN<sub>95</sub>) = 18.5332 g N/m<sup>3</sup>  
95% percentile for effluent TSS (TSS<sub>95</sub>) = 15.7415 g SS/m<sup>3</sup>

The maximum effluent total nitrogen level (18 mg N/l) was violated during 0.57292 days, i.e. 8.1845% of the operating time.  
The limit was violated at 5 different occasions.

The maximum effluent ammonia nitrogen level (4 mg N/l) was violated during 4.375 days, i.e. 62.5% of the operating time.  
The limit was violated at 7 different occasions.

\*\*\*\*\*  
\* RAINWEATHER FILE \*  
\*\*\*\*\*

Overall plant performance during time 7 to 14 days  
\*\*\*\*\*

Effluent average concentrations based on load  
-----

Effluent average flow rate = 23808.1776 m3/d  
Effluent average SI conc = 22.8388 mg COD/l  
Effluent average SS conc = 1.1349 mg COD/l  
Effluent average XI conc = 5.6339 mg COD/l  
Effluent average XS conc = 0.34502 mg COD/l  
Effluent average XBH conc = 12.8584 mg COD/l  
Effluent average XBA conc = 0.64114 mg COD/l  
Effluent average XP conc = 2.0654 mg COD/l  
Effluent average SO conc = 0.84653 mg (-COD)/l  
Effluent average SNO conc = 6.9493 mg N/l  
Effluent average SNH conc = 5.0085 mg N/l (limit = 4 mg N/l)  
Effluent average SND conc = 0.81596 mg N/l  
Effluent average XND conc = 0.023611 mg N/l  
Effluent average SALK conc = 5.1458 mol HCO3/m3  
Effluent average TSS conc = 16.1579 mg SS/l (limit = 30 mg SS/l)

Effluent average Kjeldahl N conc = 7.39 mg N/l  
Effluent average total N conc = 14.3394 mg N/l (limit = 18 mg COD/l)  
Effluent average total COD conc = 45.5175 mg COD/l (limit = 100 mg COD/l)  
Effluent average BOD5 conc = 3.4749 mg/l (limit = 10 mg/l)

Effluent average load  
-----

Effluent average SI load = 543.7504 kg COD/day  
Effluent average SS load = 27.0204 kg COD/day  
Effluent average XI load = 134.1321 kg COD/day  
Effluent average XS load = 8.2142 kg COD/day  
Effluent average XBH load = 306.1353 kg COD/day  
Effluent average XBA load = 15.2645 kg COD/day  
Effluent average XP load = 49.1729 kg COD/day  
Effluent average SO load = 20.1542 kg (-COD)/day  
Effluent average SNO load = 165.4509 kg N/day  
Effluent average SNH load = 119.244 kg N/day  
Effluent average SND load = 19.4266 kg N/day  
Effluent average XND load = 0.56215 kg N/day  
Effluent average SALK load = 122.511 kmol HCO3/day  
Effluent average TSS load = 384.6892 kg SS/day

Effluent average Kjeldahl N load = 175.943 kg N/d  
Effluent average total N load = 341.3939 kg N/d  
Effluent average total COD load = 1083.6897 kg COD/d  
Effluent average BOD5 load = 82.7306 kg/d

Other effluent quality variables  
-----

Influent Quality (I.Q.) index = 52081.3952 kg poll.units/d  
Effluent Quality (E.Q.) index = 8951.3288 kg poll.units/d

Sludge production for disposal = 16471.0731 kg SS  
Average sludge production for disposal per day = 2353.0104 kg SS/d  
Sludge production released into effluent = 2692.8242 kg SS  
Average sludge production released into effluent per day = 384.6892 kg SS/d  
Total sludge production = 19163.8973 kg SS

Total average sludge production per day = 2737.6996 kg SS/d

Total aeration energy = 23389.7067 kWh  
Average aeration energy per day = 3341.3867 kWh/d

Total pumping energy (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 2717.19 kWh  
Average pumping energy per day (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 388.17 kWh/d

Total mixing energy = 1680 kWh  
Average mixing energy per day = 240 kWh/d

Total added carbon volume = 0 m<sup>3</sup>  
Average added carbon flow rate = 0 m<sup>3</sup>/d  
Total added carbon mass = 0 kg COD  
Average added carbon mass per day = 0 kg COD/d

#### Operational Cost Index

-----  
Aeration energy cost index = 3341.3867  
Pumping energy cost index = 388.17  
Carbon source addition cost index = 0  
Mixing energy cost index = 240  
Total Operational Cost Index (OCI) = 15734.6089

#### Effluent violations

-----  
95% percentile for effluent SNH (Ammonia<sub>95</sub>) = 9.4978 g N/m<sup>3</sup>  
95% percentile for effluent TN (TN<sub>95</sub>) = 17.8121 g N/m<sup>3</sup>  
95% percentile for effluent TSS (TSS<sub>95</sub>) = 21.6824 g SS/m<sup>3</sup>

The maximum effluent total nitrogen level (18 mg N/l) was violated during 0.32292 days, i.e. 4.6131% of the operating time.  
The limit was violated at 3 different occasions.

The maximum effluent ammonia nitrogen level (4 mg N/l) was violated during 4.4375 days, i.e. 63.3929% of the operating time.  
The limit was violated at 7 different occasions.

\*\*\*\*\*  
\* STORMWEATHER FILE \*  
\*\*\*\*\*

Overall plant performance during time 7 to 14 days  
\*\*\*\*\*

Effluent average concentrations based on load

-----  
Effluent average flow rate = 20658.1004 m3/d  
Effluent average SI conc = 26.2999 mg COD/l  
Effluent average SS conc = 1.1194 mg COD/l  
Effluent average XI conc = 5.5746 mg COD/l  
Effluent average XS conc = 0.32571 mg COD/l  
Effluent average XBH conc = 11.9054 mg COD/l  
Effluent average XBA conc = 0.57344 mg COD/l  
Effluent average XP conc = 1.8527 mg COD/l  
Effluent average SO conc = 0.75549 mg (-COD)/l  
Effluent average SNO conc = 7.3707 mg N/l  
Effluent average SNH conc = 5.681 mg N/l (limit = 4 mg N/l)  
Effluent average SND conc = 0.80749 mg N/l  
Effluent average XND conc = 0.022846 mg N/l  
Effluent average SALK conc = 4.9038 mol HCO3/m3  
Effluent average TSS conc = 15.1739 mg SS/l (limit = 30 mg SS/l)  
  
Effluent average Kjeldahl N conc = 7.9553 mg N/l  
Effluent average total N conc = 15.326 mg N/l (limit = 18 mg COD/l)  
Effluent average total COD conc = 47.6511 mg COD/l (limit = 100 mg COD/l)  
Effluent average BOD5 conc = 3.2314 mg/l (limit = 10 mg/l)

Effluent average load

-----  
Effluent average SI load = 543.3052 kg COD/day  
Effluent average SS load = 23.1245 kg COD/day  
Effluent average XI load = 115.16 kg COD/day  
Effluent average XS load = 6.7285 kg COD/day  
Effluent average XBH load = 245.9427 kg COD/day  
Effluent average XBA load = 11.8463 kg COD/day  
Effluent average XP load = 38.2733 kg COD/day  
Effluent average SO load = 15.6069 kg (-COD)/day  
Effluent average SNO load = 152.2652 kg N/day  
Effluent average SNH load = 117.3594 kg N/day  
Effluent average SND load = 16.6812 kg N/day  
Effluent average XND load = 0.47195 kg N/day  
Effluent average SALK load = 101.3031 kmol HCO3/day  
Effluent average TSS load = 313.4631 kg SS/day  
  
Effluent average Kjeldahl N load = 164.3417 kg N/d  
Effluent average total N load = 316.6069 kg N/d  
Effluent average total COD load = 984.3805 kg COD/d  
Effluent average BOD5 load = 66.7547 kg/d

Other effluent quality variables

-----  
Influent Quality (I.Q.) index = 54061.497 kg poll.units/d  
Effluent Quality (E.Q.) index = 8197.7197 kg poll.units/d

Sludge production for disposal = 18252.4352 kg SS  
Average sludge production for disposal per day = 2607.4907 kg SS/d  
Sludge production released into effluent = 2194.2416 kg SS  
Average sludge production released into effluent per day = 313.4631 kg SS/d  
Total sludge production = 20446.6768 kg SS  
Total average sludge production per day = 2920.9538 kg SS/d



Total aeration energy = 23389.7067 kWh  
Average aeration energy per day = 3341.3867 kWh/d

Total pumping energy (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 2717.19 kWh  
Average pumping energy per day (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 388.17 kWh/d

Total mixing energy = 1680 kWh  
Average mixing energy per day = 240 kWh/d

Total added carbon volume = 0 m<sup>3</sup>  
Average added carbon flow rate = 0 m<sup>3</sup>/d  
Total added carbon mass = 0 kg COD  
Average added carbon mass per day = 0 kg COD/d

#### Operational Cost Index

-----  
Aeration energy cost index = 3341.3867  
Pumping energy cost index = 388.17  
Carbon source addition cost index = 0  
Mixing energy cost index = 240  
Total Operational Cost Index (OCI) = 17007.0104

#### Effluent violations

-----  
95% percentile for effluent SNH (Ammonia<sub>95</sub>) = 10.1872 g N/m<sup>3</sup>  
95% percentile for effluent TN (TN<sub>95</sub>) = 18.9449 g N/m<sup>3</sup>  
95% percentile for effluent TSS (TSS<sub>95</sub>) = 20.7485 g SS/m<sup>3</sup>

The maximum effluent total nitrogen level (18 mg N/l) was violated during 0.64583 days, i.e. 9.2262% of the operating time.  
The limit was violated at 4 different occasions.

The maximum effluent ammonia nitrogen level (4 mg N/l) was violated during 4.625 days, i.e. 66.0714% of the operating time.  
The limit was violated at 7 different occasions.

**STEADY STATE RESULTS FOR CLOSEDLOOP**

**i.e. constant input file and ideal sensors/actuators, control strategy according to BSM1 description**

**(Results from Matlab/Simulink implementation by Dr Ulf Jeppsson, IEA, Lund University, Sweden, March 28 2008)**

## Influent characteristics

\*\*\*\*\*

SI = 30 mg COD/l  
 SS = 69.5 mg COD/l  
 XI = 51.2 mg COD/l  
 XS = 202.32 mg COD/l  
 XBH = 28.17 mg COD/l  
 XBA = 0 mg COD/l  
 XP = 0 mg COD/l  
 SO = 0 mg -COD/l  
 SNO = 0 mg N/l  
 SNH = 31.56 mg N/l  
 SND = 6.95 mg N/l  
 XND = 10.59 mg N/l  
 SALK = 7 mol HCO<sub>3</sub>/m<sup>3</sup>  
 TSS = 211.2675 mg SS/l

## Flow conditions

\*\*\*\*\*

Influent flow to WWTP = 18446 m<sup>3</sup>/d  
 Influent flow to AS = 53377.6074 m<sup>3</sup>/d  
 Internal recirculation = 16485.6074 m<sup>3</sup>/d  
 Settler feed flow = 36892 m<sup>3</sup>/d  
 Returned sludge flow = 18446 m<sup>3</sup>/d  
 Wastage sludge flow = 385 m<sup>3</sup>/d  
 Effluent flow = 18061 m<sup>3</sup>/d

## Input to AS

\*\*\*\*\*

SI = 30 mg COD/l  
 SS = 24.5463 mg COD/l  
 XI = 1149.1683 mg COD/l  
 XS = 113.7148 mg COD/l  
 XBH = 2533.1267 mg COD/l  
 XBA = 151.7894 mg COD/l  
 XP = 445.766 mg COD/l  
 SO = 1.3088 mg -COD/l  
 SNO = 8.8506 mg N/l  
 SNH = 11.3461 mg N/l  
 SND = 2.8366 mg N/l  
 XND = 6.8699 mg N/l  
 SALK = 4.924 mol HCO<sub>3</sub>/m<sup>3</sup>  
 TSS = 3295.1738 mg SS/l

## Reactor 1

\*\*\*\*\*

SI = 30 mg COD/l  
 SS = 3.2439 mg COD/l  
 XI = 1149.1683 mg COD/l  
 XS = 98.6029 mg COD/l  
 XBH = 2552.1095 mg COD/l  
 XBA = 151.6721 mg COD/l  
 XP = 446.9249 mg COD/l  
 SO = 0.0076964 mg -COD/l  
 SNO = 3.5133 mg N/l  
 SNH = 11.8312 mg N/l  
 SND = 1.3621 mg N/l

XND = 6.1775 mg N/l  
SALK = 5.3399 mol HCO3/m3  
TSS = 3298.8582 mg SS/l

Reactor 2

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 1.6707 mg COD/l  
XI = 1149.1683 mg COD/l  
XS = 91.7032 mg COD/l  
XBH = 2552.3711 mg COD/l  
XBA = 151.5303 mg COD/l  
XP = 448.0839 mg COD/l  
SO = 6.0271e-05 mg -COD/l  
SNO = 1 mg N/l  
SNH = 12.5482 mg N/l  
SND = 0.78899 mg N/l  
XND = 5.9537 mg N/l  
SALK = 5.5706 mol HCO3/m3  
TSS = 3294.6425 mg SS/l

Reactor 3

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 1.2195 mg COD/l  
XI = 1149.1683 mg COD/l  
XS = 69.6594 mg COD/l  
XBH = 2560.2025 mg COD/l  
XBA = 152.6873 mg COD/l  
XP = 449.6336 mg COD/l  
SO = 1.635 mg -COD/l  
SNO = 6.2289 mg N/l  
SNH = 7.3197 mg N/l  
SND = 0.8307 mg N/l  
XND = 4.7131 mg N/l  
SALK = 4.8236 mol HCO3/m3  
TSS = 3286.0133 mg SS/l

Reactor 4

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.97326 mg COD/l  
XI = 1149.1683 mg COD/l  
XS = 54.4484 mg COD/l  
XBH = 2563.3104 mg COD/l  
XBA = 153.7108 mg COD/l  
XP = 451.1853 mg COD/l  
SO = 2.4745 mg -COD/l  
SNO = 11.0693 mg N/l  
SNH = 2.7825 mg N/l  
SND = 0.75276 mg N/l  
XND = 3.8403 mg N/l  
SALK = 4.1538 mol HCO3/m3  
TSS = 3278.8674 mg SS/l

Reactor 5

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.80801 mg COD/l  
XI = 1149.1683 mg COD/l  
XS = 44.4828 mg COD/l  
XBH = 2562.8514 mg COD/l  
XBA = 154.163 mg COD/l

XP = 452.7367 mg COD/l  
SO = 2 mg -COD/l  
SNO = 13.5243 mg N/l  
SNH = 0.67193 mg N/l  
SND = 0.6645 mg N/l  
XND = 3.2605 mg N/l  
SALK = 3.8277 mol HCO3/m3  
TSS = 3272.5516 mg SS/l

Settler underflow

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.80801 mg COD/l  
XI = 2247.1365 mg COD/l  
XS = 86.9837 mg COD/l  
XBH = 5011.5176 mg COD/l  
XBA = 301.4575 mg COD/l  
XP = 885.3022 mg COD/l  
SO = 2 mg -COD/l  
SNO = 13.5243 mg N/l  
SNH = 0.67193 mg N/l  
SND = 0.6645 mg N/l  
XND = 6.3757 mg N/l  
SALK = 3.8277 mol HCO3/m3  
TSS = 6399.2981 mg SS/l

Settler effluent

\*\*\*\*\*

SI = 30 mg COD/l  
SS = 0.80801 mg COD/l  
XI = 4.39 mg COD/l  
XS = 0.16993 mg COD/l  
XBH = 9.7905 mg COD/l  
XBA = 0.58893 mg COD/l  
XP = 1.7295 mg COD/l  
SO = 2 mg -COD/l  
SNO = 13.5243 mg N/l  
SNH = 0.67193 mg N/l  
SND = 0.6645 mg N/l  
XND = 0.012455 mg N/l  
SALK = 3.8277 mol HCO3/m3  
TSS = 12.5016 mg SS/l

Settler internal (1 is top layer)

\*\*\*\*\*

TSS1 = 12.5016 mg SS/l  
TSS2 = 18.1183 mg SS/l  
TSS3 = 29.548 mg SS/l  
TSS4 = 69.0015 mg SS/l  
TSS5 = 356.2825 mg SS/l  
TSS6 = 356.2825 mg SS/l  
TSS7 = 356.2825 mg SS/l  
TSS8 = 356.2825 mg SS/l  
TSS9 = 356.2825 mg SS/l  
TSS10 = 6399.2981 mg SS/l

Other variables

\*\*\*\*\*

Trad. sludge age (XS + XP + XI + XBH + XBA in reactors) = 7.3273 days  
Spec. sludge age (XBH + XBA in reactors and settler) = 9.139 days  
Total hydraulic retention time = 15.6118 hours  
Reactor hydraulic retention time = 7.8053 hours  
Thickening factor at bottom of settler(TSSu/TSSfeed) = 1.9554

Thinning factor at top of settler ( $TSS_{eff}/TSS_{feed}$ ) = 0.0038201

Dimensions

\*\*\*\*\*

Reactor 1 is anoxic  
Volume reactor 1 = 1000 m3  
Reactor 2 is anoxic  
Volume reactor 2 = 1000 m3  
Reactor 3 is aerobic  
Volume reactor 3 = 1333 m3  
Reactor 4 is aerobic  
Volume reactor 4 = 1333 m3  
Reactor 5 is aerobic  
Volume reactor 5 = 1333 m3  
Settler height = 4 m  
Settler area = 1500 m2  
Settler volume = 6000 m3

## DYNAMIC RESULTS FOR CLOSEDLOOP BSM1

(Results from Matlab/Simulink implementation by Dr Ulf Jeppsson, IEA, Lund University, Sweden, March 28 2008)

### SUMMARY OF PLANT PERFORMANCE

\*\*\*\*\*

The plant was simulated in closed loop for 150 days to achieve quasi steady state using the CONSTANT INPUT file (ideal sensors and actuators used). Then the DRYWEATHER file was used to simulate the closed loop dynamics during 14 days and set up the plant for the dynamic benchmark simulations (using active noise and delay on sensors and actuators). The results of this simulation was used as initial values for the actual plant performance calculations using the different dynamic input files.

#### Default controllers:

controller for DO in tank 5, DOsetpoint=2mg/l, Sensor model A, Actuator model used, Noise data from file column 1;  
controller for NO<sub>3</sub>-N in tank 2, NO<sub>3</sub>setpoint=1mg/l, Sensor model B0, Noise data from file column 2.

Evaluation is based on data every 15 minutes and uses zero-order hold (forward Euler) for integration between measurements.

\*\*\*\*\*  
\* DRYWEATHER FILE \*  
\*\*\*\*\*

#### Overall plant performance during time 7 to 14 days

\*\*\*\*\*

#### Effluent average concentrations based on load

-----

Effluent average flow rate = 18057.8774 m<sup>3</sup>/d  
Effluent average SI conc = 30 mg COD/l  
Effluent average SS conc = 0.88177 mg COD/l  
Effluent average XI conc = 4.5728 mg COD/l  
Effluent average XS conc = 0.20084 mg COD/l  
Effluent average XBH conc = 10.2314 mg COD/l  
Effluent average XBA conc = 0.57803 mg COD/l  
Effluent average XP conc = 1.7553 mg COD/l  
Effluent average SO conc = 1.9881 mg (-COD)/l  
Effluent average SNO conc = 12.4199 mg N/l  
Effluent average SNH conc = 2.5392 mg N/l (limit = 4 mg N/l)  
Effluent average SND conc = 0.70651 mg N/l  
Effluent average XND conc = 0.01442 mg N/l  
Effluent average SALK conc = 4.0409 mol HCO<sub>3</sub>/m<sup>3</sup>  
Effluent average TSS conc = 13.0038 mg SS/l (limit = 30 mg SS/l)

Effluent average Kjeldahl N conc = 4.5046 mg N/l  
Effluent average total N conc = 16.9245 mg N/l (limit = 18 mg COD/l)  
Effluent average total COD conc = 48.2201 mg COD/l (limit = 100 mg COD/l)  
Effluent average BOD<sub>5</sub> conc = 2.7568 mg/l (limit = 10 mg/l)

#### Effluent average load

-----

Effluent average SI load = 541.7363 kg COD/day  
Effluent average SS load = 15.923 kg COD/day  
Effluent average XI load = 82.5745 kg COD/day  
Effluent average XS load = 3.6267 kg COD/day  
Effluent average XBH load = 184.7574 kg COD/day  
Effluent average XBA load = 10.438 kg COD/day

Effluent average XP load = 31.6976 kg COD/day  
Effluent average SO load = 35.9017 kg (-COD)/day  
Effluent average SNO load = 224.2771 kg N/day  
Effluent average SNH load = 45.8525 kg N/day  
Effluent average SND load = 12.7581 kg N/day  
Effluent average XND load = 0.26039 kg N/day  
Effluent average SALK load = 72.9708 kmol HCO<sub>3</sub>/day  
Effluent average TSS load = 234.8206 kg SS/day

Effluent average Kjeldahl N load = 81.3429 kg N/d  
Effluent average total N load = 305.6201 kg N/d  
Effluent average total COD load = 870.7534 kg COD/d  
Effluent average BOD<sub>5</sub> load = 49.7823 kg/d

#### Other effluent quality variables

-----  
Influent Quality (I.Q.) index = 52081.3952 kg poll.units/d  
Effluent Quality (E.Q.) index = 6123.0182 kg poll.units/d

Sludge production for disposal = 17084.2397 kg SS  
Average sludge production for disposal per day = 2440.6057 kg SS/d  
Sludge production released into effluent = 1643.7439 kg SS  
Average sludge production released into effluent per day = 234.8206 kg SS/d  
Total sludge production = 18727.9836 kg SS  
Total average sludge production per day = 2675.4262 kg SS/d

Total aeration energy = 25888.4069 kWh  
Average aeration energy per day = 3698.3438 kWh/d

Total pumping energy (for Q<sub>intr</sub>, Q<sub>r</sub> and Q<sub>w</sub>) = 1687.2136 kWh  
Average pumping energy per day (for Q<sub>intr</sub>, Q<sub>r</sub> and Q<sub>w</sub>) = 241.0305 kWh/d

Total mixing energy = 1680 kWh  
Average mixing energy per day = 240 kWh/d

Total added carbon volume = 0 m<sup>3</sup>  
Average added carbon flow rate = 0 m<sup>3</sup>/d  
Total added carbon mass = 0 kg COD  
Average added carbon mass per day = 0 kg COD/d

#### Operational Cost Index

-----  
Sludge production cost index = 12203.0284  
Aeration energy cost index = 3698.3438  
Pumping energy cost index = 241.0305  
Carbon source addition cost index = 0  
Mixing energy cost index = 240  
Total Operational Cost Index (OCI) = 16382.4027

#### Effluent violations

-----  
95% percentile for effluent SNH (Ammonia<sub>95</sub>) = 7.3902 g N/m<sup>3</sup>  
95% percentile for effluent TN (TN<sub>95</sub>) = 20.2693 g N/m<sup>3</sup>  
95% percentile for effluent TSS (TSS<sub>95</sub>) = 15.7663 g SS/m<sup>3</sup>

The maximum effluent total nitrogen level (18 mg N/l) was violated during 1.2813 days, i.e. 18.3036% of the operating time.  
The limit was violated at 7 different occasions.

The maximum effluent ammonia nitrogen level (4 mg N/l) was violated during 1.1979 days, i.e. 17.1131% of the operating time.  
The limit was violated at 5 different occasions.

Performance of active controllers during time 7 to 14 days  
\*\*\*\*\*

Nitrate controller for second anoxic reactor  
=====

PI controller with anti-windup:  $K = 10000 \text{ m}^3/\text{d}/(\text{g N}/\text{m}^3)$   
 $T_i = 0.025 \text{ days}$   
 $T_t = 0.015 \text{ days}$

Controlled variable - SNO (tank 2), setpoint = 1 mg N/l  
-----

Average value of error ( $\text{mean}(e)$ ) = -0.0021211 (mg N/l)  
Average value of absolute error ( $\text{mean}(|e|)$ ) = 0.20497 (mg N/l)  
Integral of absolute error (IAE) = 1.4348 (mg N/l)\*d  
Integral of square error (ISE) = 0.56897 (mg N/l)<sup>2</sup>\*d  
Maximum absolute deviation from nitrate setpoint ( $\text{max}(e)$ ) = 0.91782 mg N/l  
Standard deviation of error ( $\text{std}(e)$ ) = 0.28509 mg N/l  
Variance of error ( $\text{var}(e)$ ) = 0.081276 (mg N/l)<sup>2</sup>

Manipulated variable (MV),  $Q_{\text{intr}}$   
-----

Maximum absolute variation of MV ( $\text{max-min}$ ) = 45734.3965 m<sup>3</sup>/d  
Maximum absolute variation of MV in one sample ( $\text{max delta}$ ) = 18918.9397 m<sup>3</sup>/d  
Average value of MV ( $\text{mean}(Q_{\text{intr}})$ ) = 18610.0822 m<sup>3</sup>/d  
Standard deviation of MV ( $\text{std}(Q_{\text{intr}})$ ) = 4078.4756 m<sup>3</sup>/d  
Variance of MV ( $\text{var}(Q_{\text{intr}})$ ) = 16633963.2296 (m<sup>3</sup>/d)<sup>2</sup>

Oxygen controller for last aerobic reactor  
=====

PI controller with anti-windup:  $K = 25 \text{ l}/\text{d}/(\text{g } (-\text{COD})/\text{m}^3)$   
 $T_i = 0.002 \text{ days}$   
 $T_t = 0.001 \text{ days}$

Controlled variable - SO (tank 5), setpoint = 2 mg (-COD)/l  
-----

Average value of error ( $\text{mean}(e)$ ) = -0.00039763 (mg (-COD)/l)  
Average value of absolute error ( $\text{mean}(|e|)$ ) = 0.084044 (mg (-COD)/l)  
Integral of absolute error (IAE) = 0.58831 (mg (-COD)/l)\*d  
Integral of square error (ISE) = 0.083975 (mg (-COD)/l)<sup>2</sup>\*d  
Maximum absolute deviation from oxygen setpoint ( $\text{max}(e)$ ) = 0.39631 mg (-COD)/l  
Standard deviation of error ( $\text{std}(e)$ ) = 0.10953 mg (-COD)/l  
Variance of error ( $\text{var}(e)$ ) = 0.011996 (mg (-COD)/l)<sup>2</sup>

Manipulated variable (MV),  $KLa$  (tank 5)  
-----

Maximum absolute variation of MV ( $\text{max-min}$ ) = 242.2831 1/d  
Maximum absolute variation of MV in one sample ( $\text{max delta}$ ) = 47.8828 1/d  
Average value of MV ( $\text{mean}(KLa_5)$ ) = 144.1219 1/d  
Standard deviation of MV ( $\text{std}(KLa_5)$ ) = 9.5682 1/d  
Variance of MV ( $\text{var}(KLa_5)$ ) = 91.5507 (1/d)<sup>2</sup>



\*\*\*\*\*  
\* RAINWEATHER FILE \*  
\*\*\*\*\*

Overall plant performance during time 7 to 14 days

\*\*\*\*\*

Effluent average concentrations based on load

-----  
Effluent average flow rate = 23806.8789 m3/d  
Effluent average SI conc = 22.8353 mg COD/l  
Effluent average SS conc = 1.0294 mg COD/l  
Effluent average XI conc = 5.6285 mg COD/l  
Effluent average XS conc = 0.31107 mg COD/l  
Effluent average XBH conc = 12.8824 mg COD/l  
Effluent average XBA conc = 0.68536 mg COD/l  
Effluent average XP conc = 2.0617 mg COD/l  
Effluent average SO conc = 1.9918 mg (-COD)/l  
Effluent average SNO conc = 9.1649 mg N/l  
Effluent average SNH conc = 3.226 mg N/l (limit = 4 mg N/l)  
Effluent average SND conc = 0.78728 mg N/l  
Effluent average XND conc = 0.021515 mg N/l  
Effluent average SALK conc = 4.8606 mol HCO3/m3  
Effluent average TSS conc = 16.1768 mg SS/l (limit = 30 mg SS/l)

Effluent average Kjeldahl N conc = 5.5816 mg N/l  
Effluent average total N conc = 14.7465 mg N/l (limit = 18 mg COD/l)  
Effluent average total COD conc = 45.4337 mg COD/l (limit = 100 mg COD/l)  
Effluent average BOD5 conc = 3.4557 mg/l (limit = 10 mg/l)

Effluent average load

-----  
Effluent average SI load = 543.6382 kg COD/day  
Effluent average SS load = 24.5064 kg COD/day  
Effluent average XI load = 133.9972 kg COD/day  
Effluent average XS load = 7.4056 kg COD/day  
Effluent average XBH load = 306.6892 kg COD/day  
Effluent average XBA load = 16.3163 kg COD/day  
Effluent average XP load = 49.0825 kg COD/day  
Effluent average SO load = 47.4177 kg (-COD)/day  
Effluent average SNO load = 218.1877 kg N/day  
Effluent average SNH load = 76.8013 kg N/day  
Effluent average SND load = 18.7426 kg N/day  
Effluent average XND load = 0.5122 kg N/day  
Effluent average SALK load = 115.7154 kmol HCO3/day  
Effluent average TSS load = 385.118 kg SS/day

Effluent average Kjeldahl N load = 132.8813 kg N/d  
Effluent average total N load = 351.069 kg N/d  
Effluent average total COD load = 1081.6353 kg COD/d  
Effluent average BOD5 load = 82.2692 kg/d

Other effluent quality variables

-----  
Influent Quality (I.Q.) index = 52081.3952 kg poll.units/  
Effluent Quality (E.Q.) index = 8184.7263 kg poll.units/d

Sludge production for disposal = 16503.104 kg SS  
Average sludge production for disposal per day = 2357.5863 kg SS/d  
Sludge production released into effluent = 2695.8261 kg SS  
Average sludge production released into effluent per day = 385.118 kg SS/d  
Total sludge production = 19198.9302 kg SS  
Total average sludge production per day = 2742.7043 kg SS/d

Total aeration energy = 25699.4632 kWh  
Average aeration energy per day = 3671.3519 kWh/d

Total pumping energy (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 1996.8482 kWh  
Average pumping energy per day (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 285.264 kWh/d

Total mixing energy = 1680 kWh  
Average mixing energy per day = 240 kWh/d

Total added carbon volume = 0 m<sup>3</sup>  
Average added carbon flow rate = 0 m<sup>3</sup>/d  
Total added carbon mass = 0 kg COD  
Average added carbon mass per day = 0 kg COD/d

#### Operational Cost Index

-----  
Sludge production cost index = 11787.9314  
Aeration energy cost index = 3671.3519  
Pumping energy cost index = 285.264  
Carbon source addition cost index = 0  
Mixing energy cost index = 240  
Total Operational Cost Index (OCI) = 15984.5473

#### Effluent violations

-----  
95% percentile for effluent SNH (Ammonia<sub>95</sub>) = 8.0395 g N/m<sup>3</sup>  
95% percentile for effluent TN (TN<sub>95</sub>) = 19.1429 g N/m<sup>3</sup>  
95% percentile for effluent TSS (TSS<sub>95</sub>) = 21.6967 g SS/m<sup>3</sup>

The maximum effluent total nitrogen level (18 mg N/l) was violated during 0.77083 days, i.e. 11.0119% of the operating time.  
The limit was violated at 5 different occasions.

The maximum effluent ammonia nitrogen level (4 mg N/l) was violated during 1.8958 days, i.e. 27.0833% of the operating time.  
The limit was violated at 8 different occasions.

#### Performance of active controllers during time 7 to 14 days \*\*\*\*\*

##### Nitrate controller for second anoxic reactor =====

PI controller with anti-windup:  $K = 10000 \text{ m}^3/\text{d}/(\text{g N}/\text{m}^3)$   
 $T_i = 0.025 \text{ days}$   
 $T_t = 0.015 \text{ days}$

Controlled variable - SNO (tank 2), setpoint = 1 mg N/l  
-----

Average value of error (mean(e)) = 0.002672 (mg N/l)  
Average value of absolute error (mean(|e|)) = 0.24784 (mg N/l)  
Integral of absolute error (IAE) = 1.7349 (mg N/l)\*d  
Integral of square error (ISE) = 0.79436 (mg N/l)<sup>2</sup>\*d  
Maximum absolute deviation from nitrate setpoint (max(e)) = 0.92134 mg N/l  
Standard deviation of error (std(e)) = 0.33686 mg N/l  
Variance of error (var(e)) = 0.11347 (mg N/l)<sup>2</sup>

Manipulated variable (MV),  $Q_{intr}$   
-----

Maximum absolute variation of MV (max-min) = 84374.4066 m<sup>3</sup>/d

Maximum absolute variation of MV in one sample (max delta) = 18678.4397 m3/d  
Average value of MV (mean(Qintr)) = 29608.9372 m3/d  
Standard deviation of MV (std(Qintr)) = 4110.5486 m3/d  
Variance of MV (var(Qintr)) = 16896609.8904 (m3/d)^2

Oxygen controller for last aerobic reactor

=====

PI controller with anti-windup: K = 25 1/d/(g (-COD)/m3)  
Ti = 0.002 days  
Tt = 0.001 days

Controlled variable - SO (tank 5), setpoint = 2 mg (-COD)/l

-----

Average value of error (mean(e)) = -0.00046529 (mg (-COD)/l)  
Average value of absolute error (mean(|e|)) = 0.079532 (mg (-COD)/l)  
Integral of absolute error (IAE) = 0.55672 (mg (-COD)/l)\*d  
Integral of square error (ISE) = 0.074733 (mg (-COD)/l)^2\*d  
Maximum absolute deviation from oxygen setpoint (max(e)) = 0.38505 mg (-COD)/l  
Standard deviation of error (std(e)) = 0.10332 mg (-COD)/l  
Variance of error (var(e)) = 0.010676 (mg (-COD)/l)^2

Manipulated variable (MV), KLa (tank 5)

-----

Maximum absolute variation of MV (max-min) = 227.3181 1/d  
Maximum absolute variation of MV in one sample (max delta) = 47.8828 1/d  
Average value of MV (mean(KLa5)) = 139.5768 1/d  
Standard deviation of MV (std(KLa5)) = 9.2235 1/d  
Variance of MV (var(KLa5)) = 85.0722 (1/d)^2

\*\*\*\*\*  
\* STORMWEATHER FILE \*  
\*\*\*\*\*

Overall plant performance during time 7 to 14 days

\*\*\*\*\*

Effluent average concentrations based on load

-----

Effluent average flow rate = 20654.9629 m3/d  
Effluent average SI conc = 26.2982 mg COD/l  
Effluent average SS conc = 0.9995 mg COD/l  
Effluent average XI conc = 5.6341 mg COD/l  
Effluent average XS conc = 0.28755 mg COD/l  
Effluent average XBH conc = 11.9051 mg COD/l  
Effluent average XBA conc = 0.63091 mg COD/l  
Effluent average XP conc = 1.9072 mg COD/l  
Effluent average SO conc = 1.9905 mg (-COD)/l  
Effluent average SNO conc = 10.553 mg N/l  
Effluent average SNH conc = 3.0622 mg N/l (limit = 4 mg N/l)  
Effluent average SND conc = 0.77656 mg N/l  
Effluent average XND conc = 0.02043 mg N/l  
Effluent average SALK conc = 4.4897 mol HCO3/m3  
Effluent average TSS conc = 15.2737 mg SS/l (limit = 30 mg SS/l)

Effluent average Kjeldahl N conc = 5.3146 mg N/l  
Effluent average total N conc = 15.8676 mg N/l (limit = 18 mg COD/l)  
Effluent average total COD conc = 47.6626 mg COD/l (limit = 100 mg COD/l)  
Effluent average BOD5 conc = 3.205 mg/l (limit = 10 mg/l)

Effluent average load

-----

Effluent average SI load = 543.1883 kg COD/day  
Effluent average SS load = 20.6447 kg COD/day  
Effluent average XI load = 116.372 kg COD/day  
Effluent average XS load = 5.9394 kg COD/day  
Effluent average XBH load = 245.8993 kg COD/day  
Effluent average XBA load = 13.0314 kg COD/day  
Effluent average XP load = 39.3935 kg COD/day  
Effluent average SO load = 41.1136 kg (-COD)/day  
Effluent average SNO load = 217.9728 kg N/day  
Effluent average SNH load = 63.2503 kg N/day  
Effluent average SND load = 16.0398 kg N/day  
Effluent average XND load = 0.42198 kg N/day  
Effluent average SALK load = 92.7345 kmol HCO3/day  
Effluent average TSS load = 315.4767 kg SS/day

Effluent average Kjeldahl N load = 109.7725 kg N/d  
Effluent average total N load = 327.7453 kg N/d  
Effluent average total COD load = 984.4686 kg COD/d  
Effluent average BOD5 load = 66.2001 kg/d

Other effluent quality variables

-----

Influent Quality (I.Q.) index = 54061.497 kg poll.units/d  
Effluent Quality (E.Q.) index = 7220.7241 kg poll.units/d

Sludge production for disposal = 18238.4311 kg SS  
Average sludge production for disposal per day = 2605.4902 kg SS/d  
Sludge production released into effluent = 2208.337 kg SS  
Average sludge production released into effluent per day = 315.4767 kg SS/d  
Total sludge production = 20446.7681 kg SS  
Total average sludge production per day = 2920.9669 kg SS/d

Total aeration energy = 26046.4214 kWh (updated BSM1 version)  
Average aeration energy per day = 3720.9173 kWh/d (updated BSM1 version)

Total pumping energy (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 1856.3886 kWh  
Average pumping energy per day (for  $Q_{intr}$ ,  $Q_r$  and  $Q_w$ ) = 265.1984 kWh/d

Total mixing energy = 1680 kWh (based on BSM2 principles)  
Average mixing energy per day = 240 kWh/d (based on BSM2 principles)

Total added carbon volume = 0 m<sup>3</sup>  
Average added carbon flow rate = 0 m<sup>3</sup>/d  
Total added carbon mass = 0 kg COD  
Average added carbon mass per day = 0 kg COD/d

#### Operational Cost Index

-----  
Sludge production cost index = 13027.4508  
Aeration energy cost index = 3720.9173  
Pumping energy cost index = 265.1984  
Carbon source addition cost index = 0  
Mixing energy cost index = 240  
Total Operational Cost Index (OCI) = 17253.5665

#### Effluent violations

-----  
95% percentile for effluent SNH (Ammonia95) = 7.8033 g N/m<sup>3</sup>  
95% percentile for effluent TN (TN95) = 20.1257 g N/m<sup>3</sup>  
95% percentile for effluent TSS (TSS95) = 20.7886 g SS/m<sup>3</sup>

The maximum effluent total nitrogen level (18 mg N/l) was violated during 1.0938 days, i.e. 15.625% of the operating time.  
The limit was violated at 7 different occasions.

The maximum effluent ammonia nitrogen level (4 mg N/l) was violated during 1.8854 days, i.e. 26.9345% of the operating time.  
The limit was violated at 7 different occasions.

The maximum effluent total suspended solids level (30 mg SS/l) was violated during 0.020833 days, i.e. 0.29762% of the operating time.  
The limit was violated at 2 different occasions.

Performance of active controllers during time 7 to 14 days  
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#### Nitrate controller for second anoxic reactor

=====

PI controller with anti-windup:  $K = 10000 \text{ m}^3/\text{d}/(\text{g N}/\text{m}^3)$   
 $T_i = 0.025 \text{ days}$   
 $T_t = 0.015 \text{ days}$

Controlled variable - SNO (tank 2), setpoint = 1 mg N/l

-----  
Average value of error (mean(e)) = 0.0051026 (mg N/l)  
Average value of absolute error (mean(|e|)) = 0.23979 (mg N/l)  
Integral of absolute error (IAE) = 1.6785 (mg N/l)\*d  
Integral of square error (ISE) = 0.78797 (mg N/l)<sup>2</sup>\*d  
Maximum absolute deviation from nitrate setpoint (max(e)) = 1.2014 mg N/l  
Standard deviation of error (std(e)) = 0.33547 mg N/l  
Variance of error (var(e)) = 0.11254 (mg N/l)<sup>2</sup>

Manipulated variable (MV), Qintr

-----  
Maximum absolute variation of MV (max-min) = 83663.6739 m3/d  
Maximum absolute variation of MV in one sample (max delta) = 18489.0489 m3/d  
Average value of MV (mean(Qintr)) = 24623.036 m3/d  
Standard deviation of MV (std(Qintr)) = 4141.7466 m3/d  
Variance of MV (var(Qintr)) = 17154064.5203 (m3/d)^2

Oxygen controller for last aerobic reactor

=====

PI controller with anti-windup: K = 25 1/d/(g (-COD)/m3)  
Ti = 0.002 days  
Tt = 0.001 days

Controlled variable - SO (tank 5), setpoint = 2 mg (-COD)/l

-----

Average value of error (mean(e)) = -0.00038723 (mg (-COD)/l)  
Average value of absolute error (mean(|e|)) = 0.080854 (mg (-COD)/l)  
Integral of absolute error (IAE) = 0.56598 (mg (-COD)/l)\*d  
Integral of square error (ISE) = 0.078876 (mg (-COD)/l)^2\*d  
Maximum absolute deviation from oxygen setpoint (max(e)) = 0.37924 mg (-COD)/l  
Standard deviation of error (std(e)) = 0.10615 mg (-COD)/l  
Variance of error (var(e)) = 0.011268 (mg (-COD)/l)^2

Manipulated variable (MV), KLa (tank 5)

-----

Maximum absolute variation of MV (max-min) = 244.5373 1/d  
Maximum absolute variation of MV in one sample (max delta) = 47.8829 1/d  
Average value of MV (mean(KLa5)) = 147.9338 1/d  
Standard deviation of MV (std(KLa5)) = 9.3809 1/d  
Variance of MV (var(KLa5)) = 88.0009 (1/d)^2